Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 2, \ 0 < t \\ u \left(0, t \right) = u \left(2, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{bmatrix} -3 & x & 0 \le x \le 1 \\ 3 & x - 6 & 1 \le x \le 2 \end{bmatrix} & 0 \le x \le 2 \\ 0 & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point $x = \frac{7}{5}$

and the moment t=0.6 by means of a Fourier series of order 12.

1)
$$u(\frac{7}{5}, 0.6) = -3.38388$$

2)
$$u(\frac{7}{5}, 0.6) = 3.07186$$

3)
$$u(\frac{7}{5}, 0.6) = -3.66251$$

4)
$$u(\frac{7}{5}, 0.6) = -1.01558 \times 10^{-10}$$

5)
$$u(\frac{7}{5}, 0.6) = -8.30552$$

Exercise 2

$$\begin{cases} \frac{\partial^2 u}{\partial t^2} \left(\mathbf{x}, \mathbf{t} \right) = 16 \frac{\partial^2 u}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ \mathbf{u} \left(\mathbf{0}, \mathbf{t} \right) = \mathbf{u} \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \leq \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \begin{cases} -\mathbf{x} & 0 \leq \mathbf{x} \leq \mathbf{1} \\ 6 \, \mathbf{x} - \mathbf{7} & 1 \leq \mathbf{x} \leq \mathbf{2} \\ -\frac{5 \, \mathbf{x}}{\pi - 2} + \frac{10}{\pi - 2} + \mathbf{5} & 2 \leq \mathbf{x} \leq \pi \end{cases} \\ \frac{\partial}{\partial \mathbf{t}} \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = -\left(\left(\mathbf{x} - \mathbf{1} \right) \, \mathbf{x} \, \left(\mathbf{x} - \pi \right)^2 \right) & \mathbf{0}. \leq \mathbf{x} \leq \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the position of the string at x=2

and the moment t=0.9 by means of a Fourier series of order 11.

1)
$$u(2,0.9) = 1.55028$$

2)
$$u(2,0.9) = -1.61245$$

3)
$$u(2,0.9) = -0.303755$$

4)
$$u(2,0.9) = 8.43289$$

5)
$$u(2,0.9) = -0.874755$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 4 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = - \left(\left(x - 3 \right) \left(x - 2 \right) \left(x^2 \left(x - \pi \right)^2 \right) & 0 \le x \le \pi \\ 0 & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.4 by means of a Fourier series of order 12.

- 1) u(1,0.4) = 5.11108
- 2) u(1,0.4) = 6.67833
- 3) u(1,0.4) = -1.74354
- 4) u(1,0.4) = -0.815826
- 5) u(1,0.4) = 5.55431

Exercise 2

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = \mathbf{16} \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \mathbf{3}, \ 0 < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{3}, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \mathbf{3} \left(\mathbf{x} - \mathbf{3} \right)^2 \left(\mathbf{x} - \mathbf{1} \right) \mathbf{x}^2 & \mathbf{0} \le \mathbf{x} \le \mathbf{3} \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.2 by means of a Fourier series of order 9.

- 1) u(1,0.2) = 3.1908
- 2) u(1,0.2) = -0.942323
- 3) u(1,0.2) = 3.979
- 4) u(1,0.2) = -0.95758
- 5) u(1,0.2) = 0.33488

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 9 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 5, 0 < t \\ u(0,t) = u(5,t) = 0 & 0 \le t \\ u(x,0) = 2 (x-5)^2 (x-1) x^2 & 0 \le x \le 5 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=4 and the moment t=0.4 by means of a Fourier series of order 10.

- 1) u(4,0.4) = 14.9873
- 2) u(4,0.4) = 7.57727
- 3) u(4,0.4) = 5.39763
- 4) u(4,0.4) = 3.92912
- 5) u(4,0.4) = -6.39456

Exercise 2

Compute the position of the string at x=1 and the moment t=0.8 by means of a Fourier series of order 9.

- 1) u(1,0.8) = 5.94216
- 2) u(1,0.8) = 2.88336
- 3) u(1,0.8) = 2.13768
- 4) u(1,0.8) = 4.98318
- 5) u(1,0.8) = 8.11306

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 25 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ u(0,t) = u(\pi,t) = 0 & 0 \le t \end{cases}$$

$$\begin{cases} u(x,0) = \begin{cases} -2x & 0 \le x \le 3 \\ \frac{6x}{\pi-3} - \frac{18}{\pi-3} - 6 & 3 \le x \le \pi \end{cases} & 0 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.9 by means of a Fourier series of order 12.

- 1) u(1,0.9) = -7.78968
- 2) $u(1,0.9) = -5.67572 \times 10^{-10}$
- 3) u(1,0.9) = -4.77518
- 4) u(1,0.9) = 2.08331
- 5) u(1,0.9) = -4.82299

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} (x,t) = 9 \frac{\partial^{2} u}{\partial x^{2}} (x,t) & 0 < x < 4, \ 0 < t \\ u(0,t) = u(4,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} 2x & 0 \le x \le 2 \\ 8 - 2x & 2 \le x \le 4 \end{cases} & 0 \le x \le 4 \\ \frac{\partial}{\partial t} u(x,0) = \begin{cases} -\frac{7x}{2} & 0 \le x \le 2 \\ 16x - 39 & 2 \le x \le 3 \\ 36 - 9x & 3 \le x \le 4 \end{cases} & 0. \le x \le 4 \\ 0 & True \end{cases}$$

Compute the position of the string at x=1 and the moment t=0.4 by means of a Fourier series of order 9.

- 1) u(1,0.4) = 2.88226
- 2) u(1,0.4) = 5.78434
- 3) u(1,0.4) = 0.290312
- 4) u(1,0.4) = 7.61393
- 5) u(1,0.4) = -2.76143

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 5, \ 0 < t \\ u(0,t) = u(5,t) = 0 & 0 \le t \end{cases}$$

$$\begin{cases} u(x,0) = \begin{cases} -\frac{8x}{3} & 0 \le x \le 3 \\ 4x - 20 & 3 \le x \le 5 \end{cases} & 0 \le x \le 5 \end{cases}$$

Compute the temperature of the bar at the point x=4 and the moment t=0.4 by means of a Fourier series of order 10.

- 1) u(4,0.4) = 2.7966
- 2) u(4,0.4) = -3.60583
- 3) u(4,0.4) = 2.07023
- 4) u(4,0.4) = 7.77069
- 5) u(4,0.4) = 2.62051

Exercise 2

$$\begin{bmatrix} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = 4 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \quad 0 < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \leq \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \begin{bmatrix} 2 \mathbf{x} & 0 \leq \mathbf{x} \leq \mathbf{2} \\ -\frac{4 \mathbf{x}}{\pi - 2} + \frac{8}{\pi - 2} + 4 & 2 \leq \mathbf{x} \leq \pi \end{bmatrix} & 0 \leq \mathbf{x} \leq \pi \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.2 by means of a Fourier series of order 8.

- 1) u(2,0.2) = 0.00640819
- 2) u(2,0.2) = -3.91831
- 3) u(2,0.2) = -4.63252
- 4) u(2,0.2) = 2.13257
- 5) u(2,0.2) = 2.65926

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = 25 \frac{\partial^2 u}{\partial x^2}(x,t) & 0 < x < 2, 0 < t \\ u(0,t) = u(2,t) = 0 & 0 \le t \\ u(x,0) = -(x-2)^2(x-1)x^2 & 0 \le x \le 2 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point $x = -\frac{8}{5}$

and the moment t=0.2 by means of a Fourier series of order 9.

1)
$$u(\frac{8}{5}, 0.2) = -5.30428$$

2)
$$u(\frac{8}{5}, 0.2) = 7.12691$$

3)
$$u(\frac{8}{5}, 0.2) = 5.56414$$

4)
$$u(\frac{8}{5}, 0.2) = 0$$

5)
$$u(\frac{8}{5}, 0.2) = -0.756228$$

Exercise 2

Compute the position of the string at x=2 and the moment t=0.2 by means of a Fourier series of order 12.

- 1) u(2,0.2) = -5.92808
- 2) u(2,0.2) = 3.1985
- 3) u(2,0.2) = -8.60175
- 4) u(2,0.2) = 6.06592
- 5) u(2,0.2) = -0.82046

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 4 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 1, \ 0 < t \\ u \left(\theta, t \right) = u \left(1, t \right) = \theta & 0 \le t \\ u \left(x, \theta \right) = 3 \left(x - 1 \right) \left(x - \frac{1}{5} \right) x & 0 \le x \le 1 \\ \theta & True \end{cases}$$

Compute the temperature of the bar at the point $x = \frac{9}{10}$

and the moment t=0.3 by means of a Fourier series of order 10.

1)
$$u(\frac{9}{10}, 0.3) = 5.48906$$

2)
$$u(\frac{9}{10}, 0.3) = -5.1557 \times 10^{-7}$$

3)
$$u(\frac{9}{10}, 0.3) = 5.44783$$

4)
$$u(\frac{9}{10}, 0.3) = 6.60163$$

5)
$$u(\frac{9}{10}, 0.3) = 3.72816$$

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 25 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (\pi,t) = 0 & 0 \le t \\ u(x,0) = \begin{bmatrix} -3x & 0 \le x \le 1 \\ \frac{3x}{\pi-1} - \frac{3}{\pi-1} - 3 & 1 \le x \le \pi \\ 0 & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.2 by means of a Fourier series of order 8.

- 1) u(1,0.2) = -1.5018
- 2) u(1,0.2) = 3.05632
- 3) u(1,0.2) = 1.58776
- 4) u(1,0.2) = 0.947156
- 5) u(1,0.2) = 2.27169

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = 4 \frac{\partial^2 u}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \quad 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = 0 & 0 \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = - \left(\left(\mathbf{x} - \mathbf{1} \right) \mathbf{x} \left(\mathbf{x} - \pi \right)^2 \right) & 0 \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.4 by means of a Fourier series of order 9.

- 1) u(2,0.4) = 7.72426
- 2) u(2,0.4) = -2.63295
- 3) u(2,0.4) = -2.89083
- 4) u(2,0.4) = -0.263495
- 5) u(2,0.4) = 1.19739

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 4 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 3, 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (3,t) = 0 & 0 \le t \\ u(x,0) = \begin{bmatrix} 7x & 0 \le x \le 1 \\ 15 - 8x & 1 \le x \le 2 & 0 \le x \le 3 \\ x - 3 & 2 \le x \le 3 \end{bmatrix}$$
True

Compute the temperature of the bar at the point x=1 and the moment t=0.7 by means of a Fourier series of order 11.

- 1) u(1,0.7) = 0.828779
- 2) u(1,0.7) = -4.28963
- 3) u(1,0.7) = 0.133154
- 4) u(1,0.7) = -1.82114
- 5) u(1,0.7) = 2.05641

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = 9 \frac{\partial^2 u}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = 0 & 0 \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = \begin{cases} 4 x & 0 \le x \le 1 \\ 3 x + 1 & 1 \le x \le 2 \\ -\frac{7 x}{\pi - 2} + \frac{14}{\pi - 2} + 7 & 2 \le x \le \pi \end{cases}$$
 True

Compute the temperature of the bar at the point x=2 and the moment t=0.6 by means of a Fourier series of order 10.

- 1) u(2,0.6) = 0.675949
- 2) u(2,0.6) = 8.58555
- 3) u(2,0.6) = -5.59146
- 4) u(2,0.6) = 0.0239099
- 5) u(2,0.6) = 1.65502

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 4 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (\pi,t) = \theta & 0 \le t \\ u(x,\theta) = \begin{bmatrix} -3x & 0 \le x \le 1 \\ \frac{3x}{\pi-1} - \frac{3}{\pi-1} - 3 & 1 \le x \le \pi \end{bmatrix} & 0 \le x \le \pi \\ \theta & True \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.6 by means of a Fourier series of order 10.

- 1) u(2,0.6) = -4.62715
- 2) u(2,0.6) = -2.40536
- 3) u(2,0.6) = 1.63071
- 4) u(2,0.6) = -1.48133
- 5) u(2,0.6) = -0.272154

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 4 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \left(x - 3 \right) \left(x - 1 \right) x \left(x - \pi \right)^2 & 0 \le x \le \pi \\ 0 & True \\ \end{bmatrix}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.8 by means of a Fourier series of order 11.

- 1) u(1,0.8) = -4.41119
- 2) u(1,0.8) = -6.6851
- 3) u(1,0.8) = 1.33896
- 4) u(1,0.8) = -5.13403
- 5) u(1,0.8) = -0.0404162

Exercise 2

$$\begin{bmatrix} \frac{\partial^2 \mathbf{u}}{\partial \mathbf{t}^2} \ (\mathbf{x}, \mathbf{t}) = 4 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \ (\mathbf{x}, \mathbf{t}) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ \mathbf{u} \ (\mathbf{0}, \mathbf{t}) = \mathbf{u} \ (\pi, \mathbf{t}) = \mathbf{0} & 0 \le \mathbf{t} \\ \mathbf{u} \ (\mathbf{x}, \mathbf{0}) = \begin{bmatrix} -\frac{x}{2} & 0 \le x \le 2 \\ \frac{x}{\pi - 2} - \frac{2}{\pi - 2} - 1 & 2 \le x \le \pi \end{bmatrix} & 0 \le \mathbf{x} \le \pi \\ \frac{\partial}{\partial \mathbf{t}} \mathbf{u} \ (\mathbf{x}, \mathbf{0}) = \begin{bmatrix} -x & 0 \le x \le 1 \\ \frac{x}{\pi - 1} - \frac{1}{\pi - 1} - 1 & 1 \le x \le \pi \end{bmatrix} & 0 \cdot \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the position of the string at x=1 and the moment t=1. by means of a Fourier series of order 10.

- 1) u(1,1) = 1.79577
- 2) u(1,1) = 3.11527
- 3) u(1,1) = 8.15689
- 4) u(1,1.) = -3.66521
- 5) u(1,1) = -0.0775097

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{cases} -x & 0 \le x \le 2 \\ 8 - 5 x & 2 \le x \le 3 \\ \frac{7 x}{\pi - 3} - \frac{21}{\pi - 3} - 7 & 3 \le x \le \pi \end{cases} & 0 \le x \le \pi$$

Compute the temperature of the bar at the point x=2 and the moment t=0.8 by means of a Fourier series of order 10.

- 1) u(2,0.8) = 4.88257
- 2) u(2,0.8) = -1.19788
- 3) $u(2,0.8) = -6.46457 \times 10^{-6}$
- 4) u(2,0.8) = -0.849051
- 5) u(2,0.8) = -3.3919

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (\mathbf{x}, \mathbf{t}) = \frac{\partial^2 u}{\partial \mathbf{x}^2} (\mathbf{x}, \mathbf{t}) & \mathbf{0} < \mathbf{x} < \pi, \ \mathbf{0} < \mathbf{t} \\ \frac{\partial u}{\partial \mathbf{x}} (\mathbf{0}, \mathbf{t}) = \frac{\partial u}{\partial \mathbf{x}} (\pi, \mathbf{t}) = \mathbf{0} & \mathbf{0} \le \mathbf{t} \\ \mathbf{u} (\mathbf{x}, \mathbf{0}) = \begin{cases} -4 \mathbf{x} & \mathbf{0} \le \mathbf{x} \le \mathbf{1} \\ -\mathbf{x} - \mathbf{3} & \mathbf{1} \le \mathbf{x} \le \mathbf{2} \\ \frac{5 \mathbf{x}}{\pi - 2} - \frac{10}{\pi - 2} - \mathbf{5} & \mathbf{2} \le \mathbf{x} \le \pi \end{cases}$$

$$\mathbf{0} \qquad \qquad \mathbf{True}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.7 by means of a Fourier series of order 9.

- 1) u(1,0.7) = -1.60434
- 2) u(1,0.7) = 1.1892
- 3) u(1,0.7) = 0.521932
- 4) u(1,0.7) = 0.291703
- 5) u(1,0.7) = -2.98942

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 16 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ u(0,t) = u(\pi,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -9x & 0 \le x \le 1 \\ \frac{9x}{\pi-1} - \frac{9}{\pi-1} - 9 & 1 \le x \le \pi \end{cases} & 0 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.6 by means of a Fourier series of order 10.

- 1) u(2,0.6) = -1.5539
- 2) u(2,0.6) = -8.66491
- 3) u(2,0.6) = -0.000435566
- 4) u(2,0.6) = -6.48636
- 5) u(2,0.6) = -6.72479

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 4 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 5, \ 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (5,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -\frac{x}{3} & 0 \le x \le 3 \\ \frac{x}{2} - \frac{5}{2} & 3 \le x \le 5 \end{cases} & 0 \le x \le 5 \\ 0 & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=4 and the moment t=0.2 by means of a Fourier series of order 10.

- 1) u(4,0.2) = 2.47748
- 2) u(4,0.2) = 3.01623
- 3) u(4,0.2) = 2.53901
- 4) u(4,0.2) = -0.522824
- 5) u(4,0.2) = -4.17438

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}\left(x,t\right) = 16\frac{\partial^{2}u}{\partial x^{2}}\left(x,t\right) & 0 < x < \pi, \quad 0 < t \\ u\left(0,t\right) = u\left(\pi,t\right) = 0 & 0 \leq t \\ u\left(x,0\right) = 2\left(x-1\right)x\left(x-\pi\right) & 0 \leq x \leq \pi \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.2 by means of a Fourier series of order 9.

- 1) u(2,0.2) = -7.73585
- 2) u(2,0.2) = 3.13808
- 3) u(2,0.2) = -0.107756
- 4) u(2,0.2) = 4.53022
- 5) u(2,0.2) = 3.63693

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} \left(x, t \right) = 25 \frac{\partial^{2} u}{\partial x^{2}} \left(x, t \right) & 0 < x < 1, \ 0 < t \\ u \left(0, t \right) = u \left(1, t \right) = 0 & 0 \le t \\ \\ u \left(x, 0 \right) = \begin{cases} 60 \ x & 0 \le x \le \frac{1}{10} \\ 20 - 140 \ x & \frac{1}{10} \le x \le \frac{1}{5} \\ 10 \ x - 10 & \frac{1}{5} \le x \le 1 \end{cases} & 0 \le x \le 1 \\ \\ \frac{\partial}{\partial t} u \left(x, 0 \right) = -3 \ \left(x - 1 \right) \ \left(x - \frac{3}{10} \right) \ \left(x - \frac{1}{10} \right) \ x & 0. \le x \le 1 \\ 0 & \text{True} \end{cases}$$

Compute the position of the string at $x = \frac{1}{10}$

and the moment t=0.1 by means of a Fourier series of order 8.

1)
$$u(\frac{1}{10}, 0.1) = 2.73897$$

2)
$$u(\frac{1}{10}, 0.1) = 3.27652$$

3)
$$u(\frac{1}{10}, 0.1) = 0.971827$$

4)
$$u(\frac{1}{10}, 0.1) = -5.27863$$

5)
$$u(\frac{1}{10}, 0.1) = -4.80909$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 9 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{cases} -x & 0 \le x \le 1 \\ 5 x - 6 & 1 \le x \le 2 \\ -\frac{4x}{\pi - 2} + \frac{8}{\pi - 2} + 4 & 2 \le x \le \pi \end{cases}$$
 True

Compute the temperature of the bar at the point x=1 and the moment t=0.2 by means of a Fourier series of order 8.

- 1) u(1,0.2) = 0.23636
- 2) u(1,0.2) = -7.85146
- 3) u(1,0.2) = -7.77485
- 4) u(1,0.2) = 6.75614
- 5) u(1,0.2) = -2.8286

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 9 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 3, 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (3,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -x & 0 \le x \le 1 \\ 2x - 3 & 1 \le x \le 2 & 0 \le x \le 3 \\ 3 - x & 2 \le x \le 3 \end{cases} \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=1. by means of a Fourier series of order 8.

- 1) u(2,1.) = 2.07378
- 2) u(2,1) = 1.8126
- 3) u(2,1) = 0.000015722
- 4) u(2,1) = -4.16633
- 5) u(2,1.) = 0.835338

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{cases} 3 x & 0 \le x \le 3 \\ -\frac{9 x}{\pi - 3} + \frac{27}{\pi - 3} + 9 & 3 \le x \le \pi \end{cases} & 0 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.6 by means of a Fourier series of order 8.

- 1) u(2,0.6) = 7.68876
- 2) u(2,0.6) = 0.00036828
- 3) u(2,0.6) = 4.62837
- 4) u(2,0.6) = 4.66209
- 5) u(2,0.6) = 1.51416

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ \frac{\partial u}{\partial x} \left(\theta, t \right) = \frac{\partial u}{\partial x} \left(\pi, t \right) = \theta & 0 \le t \\ u \left(x, \theta \right) = \left(x - 3 \right) \left(x - 2 \right) x^2 \left(x - \pi \right)^2 & 0 \le x \le \pi \\ \theta & True \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.7 by means of a Fourier series of order 9.

- 1) u(2,0.7) = -4.84068
- 2) u(2,0.7) = 2.37758
- 3) u(2,0.7) = 3.13624
- 4) u(2,0.7) = -1.12844
- 5) u(2,0.7) = -4.98738

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(\theta, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, \theta \right) = \begin{cases} \frac{4 x}{3} & 0 \le x \le 3 \\ -\frac{4 x}{\pi - 3} + \frac{12}{\pi - 3} + 4 & 3 \le x \le \pi \end{cases} & 0 \le x \le \pi$$

Compute the temperature of the bar at the point x=1 and the moment t=0.9 by means of a Fourier series of order 11.

1)
$$u(1,0.9) = 1.24657 \times 10^{-6}$$

2)
$$u(1,0.9) = 3.29973$$

3)
$$u(1,0.9) = 7.45885$$

4)
$$u(1,0.9) = -2.01698$$

5)
$$u(1,0.9) = -5.51777$$

Exercise 2

$$\begin{bmatrix} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = 4 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < 1, \ 0 < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{1}, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \left(\mathbf{x} - \mathbf{1} \right) \ \left(\mathbf{x} - \frac{1}{5} \right) \ \mathbf{x}^2 & 0 \le \mathbf{x} \le \mathbf{1} \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point $x = \frac{3}{5}$

and the moment t=0.9 by means of a Fourier series of order 12.

1)
$$u(\frac{3}{5}, 0.9) = -0.0333333$$

2)
$$u(\frac{3}{5}, 0.9) = -1.59038$$

3)
$$u(\frac{3}{5}, 0.9) = -1.10033$$

4)
$$u(\frac{3}{5}, 0.9) = 1.32086$$

5)
$$u(\frac{3}{5}, 0.9) = -3.66562$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 25 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 2, \ 0 < t \\ u(0,t) = u(2,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} 6x & 0 \le x \le 1 \\ 12 - 6x & 1 \le x \le 2 \end{cases} & 0 \le x \le 2 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point $x = \frac{3}{2}$

and the moment $t\!=\!\,0.8\,$ by means of a Fourier series of order $\,9$.

1)
$$u(\frac{3}{2}, 0.8) = 1.29988$$

2)
$$u(\frac{3}{2}, 0.8) = 5.6026$$

3)
$$u(\frac{3}{2}, 0.8) = 0$$

4)
$$u(\frac{3}{2}, 0.8) = 4.61292$$

5)
$$u(\frac{3}{2}, 0.8) = 4.68073$$

Exercise 2

$$\begin{bmatrix} \frac{\partial^2 u}{\partial t^2} \left(\mathbf{x}, \mathbf{t} \right) = 4 \frac{\partial^2 u}{\partial x^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ \mathbf{u} \left(\mathbf{0}, \mathbf{t} \right) = \mathbf{u} \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \leq \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \begin{cases} -\mathbf{x} & 0 \leq \mathbf{x} \leq \mathbf{1} \\ \frac{\mathbf{x}}{\pi - 1} - \frac{1}{\pi - 1} - \mathbf{1} & 1 \leq \mathbf{x} \leq \pi \end{cases} & 0 \leq \mathbf{x} \leq \pi \\ \frac{\partial}{\partial t} \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \begin{cases} -8 \mathbf{x} & 0 \leq \mathbf{x} \leq \mathbf{1} \\ 17 \mathbf{x} - 25 & 1 \leq \mathbf{x} \leq \mathbf{2} \\ -\frac{9 \mathbf{x}}{\pi - 2} + \frac{18}{\pi - 2} + 9 & 2 \leq \mathbf{x} \leq \pi \end{cases} & \mathbf{0}.$$

Compute the position of the string at x=1

and the moment t=1. by means of a Fourier series of order 11.

1)
$$u(1,1) = -7.92645$$

2)
$$u(1,1) = 1.83855$$

3)
$$u(1,1) = -2.68272$$

4)
$$u(1,1) = -5.14295$$

5)
$$u(1,1.) = 7.52021$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = 16 \frac{\partial^2 u}{\partial x^2}(x,t) & 0 < x < 3, 0 < t \\ u(0,t) = u(3,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} 8x & 0 \le x \le 1 \\ 12 - 4x & 1 \le x \le 3 \end{cases} & 0 \le x \le 3 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.3 by means of a Fourier series of order 8.

- 1) u(1,0.3) = 0.0283178
- 2) u(1,0.3) = 7.10309
- 3) u(1,0.3) = 5.69885
- 4) u(1,0.3) = -3.38656
- 5) u(1,0.3) = 0.570121

Exercise 2

Compute the position of the string at x=4 and the moment t=0.6 by means of a Fourier series of order 10.

- 1) u(4,0.6) = 2.66471
- 2) u(4,0.6) = 6.29193
- 3) u(4,0.6) = -1.08334
- 4) u(4,0.6) = 7.13053
- 5) u(4,0.6) = -5.35081

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 25 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 4, \ 0 < t \\ u \left(0, t \right) = u \left(4, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = - \left(x - 4 \right)^2 \left(x - 1 \right) x & 0 \le x \le 4 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.5 by means of a Fourier series of order 9.

- 1) u(1,0.5) = -2.5204
- 2) u(1,0.5) = 4.58933
- 3) u(1,0.5) = 3.55925
- 4) u(1,0.5) = -0.0019012
- 5) u(1,0.5) = 6.84878

Exercise 2

$$\begin{bmatrix} \frac{\partial^2 u}{\partial t^2} \left(\mathbf{X}, \mathbf{t} \right) = 9 \frac{\partial^2 u}{\partial x^2} \left(\mathbf{X}, \mathbf{t} \right) & 0 < \mathbf{X} < \mathbf{4}, \ 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\mathbf{4}, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ u \left(\mathbf{X}, \mathbf{0} \right) = -3 \left(\mathbf{X} - \mathbf{4} \right) \left(\mathbf{X} - \mathbf{2} \right) \mathbf{X} & 0 \le \mathbf{X} \le \mathbf{4} \\ \frac{\partial}{\partial \mathbf{t}} u \left(\mathbf{X}, \mathbf{0} \right) = \begin{cases} -8 \, \mathbf{X} & 0 \le \mathbf{X} \le \mathbf{1} \\ \frac{8 \, \mathbf{X}}{3} - \frac{32}{3} & \mathbf{1} \le \mathbf{X} \le \mathbf{4} \end{cases} & \mathbf{0}. \le \mathbf{X} \le \mathbf{4} \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the position of the string at x=3 and the moment t=0.4 by means of a Fourier series of order 11.

- 1) u(3,0.4) = 0.756349
- 2) u(3,0.4) = -4.2899
- 3) u(3,0.4) = -7.73235
- 4) u(3,0.4) = 2.96945
- 5) u(3,0.4) = 7.8466

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = \frac{\partial^2 u}{\partial x^2}(x,t) & 0 < x < \pi, \ 0 < t \\ u(\theta,t) = u(\pi,t) = \theta & 0 \le t \end{cases}$$

$$\begin{cases} u(x,\theta) = \begin{cases} \frac{x}{2} & 0 \le x \le 2 \\ 2x - 3 & 2 \le x \le 3 \ 0 \le x \le \pi \\ -\frac{3x}{\pi - 3} + \frac{9}{\pi - 3} + 3 \ 3 \le x \le \pi \end{cases}$$

$$\begin{cases} 0 & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.2 by means of a Fourier series of order 9.

- 1) u(1,0.2) = -7.32307
- 2) u(1,0.2) = 0.520476
- 3) u(1,0.2) = 1.09239
- 4) u(1,0.2) = 7.82344
- 5) u(1,0.2) = 8.6156

Exercise 2

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = 4 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\pi, \mathbf{t} \right) = 0 & 0 \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \begin{cases} -9 \ \mathbf{x} & 0 \le \mathbf{x} \le 1 \\ 8 \ \mathbf{x} - 17 & 1 \le \mathbf{x} \le 2 \\ \frac{\mathbf{x}}{\pi - 2} - \frac{2}{\pi - 2} - 1 & 2 \le \mathbf{x} \le \pi \end{cases}$$

$$\mathbf{0} \qquad \qquad \qquad \mathbf{True}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.6 by means of a Fourier series of order 9.

- 1) u(1,0.6) = 3.52019
- 2) u(1,0.6) = 3.10012
- 3) u(1,0.6) = -4.27712
- 4) u(1,0.6) = -2.46604
- 5) u(1,0.6) = -3.33131

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = \mathbf{16} \frac{\partial^2 u}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = \begin{cases} -\mathbf{x} & 0 \le \mathbf{x} \le \mathbf{1} \\ \frac{\mathbf{x}}{\pi - \mathbf{1}} - \frac{1}{\pi - \mathbf{1}} - \mathbf{1} & \mathbf{1} \le \mathbf{x} \le \pi \end{cases} & 0 \le \mathbf{x} \le \pi$$

Compute the temperature of the bar at the point x=1 and the moment t=0.1 by means of a Fourier series of order 10.

- 1) u(1,0.1) = -5.53154
- 2) u(1,0.1) = -2.818
- 3) u(1,0.1) = -0.133827
- 4) u(1,0.1) = 7.59563
- 5) u(1,0.1) = 5.06097

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 9 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 4, 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (4,t) = 0 & 0 \le t \\ u(x,0) = 3 (x-4)^2 (x-2) (x-1) x^2 & 0 \le x \le 4 \\ 0 & True \end{bmatrix}$$

Compute the temperature of the bar at the point x=3 and the moment t=1. by means of a Fourier series of order 10.

- 1) u(3,1.) = -4.0482
- 2) u(3,1.) = 3.86538
- 3) u(3,1.) = 0.185041
- 4) u(3,1) = -3.11604
- 5) u(3,1) = 14.6835

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \quad 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = -2 \left(x - 2 \right) x \left(x - \pi \right)^2 & 0 \le x \le \pi \\ 0 & \text{True} \\ \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.6 by means of a Fourier series of order 10.

- 1) u(2,0.6) = -5.67526
- 2) u(2,0.6) = 0.000317165
- 3) u(2,0.6) = 2.41329
- 4) u(2,0.6) = 5.22621
- 5) u(2,0.6) = 5.40698

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t}\left(x,t\right)=16\frac{\partial^{2} u}{\partial x^{2}}\left(x,t\right) & 0< x< 5, \ 0< t \\ \frac{\partial u}{\partial x}\left(0,t\right)=\frac{\partial u}{\partial x}\left(5,t\right)=0 & 0\leq t \\ u\left(x,0\right)=2\left(x-5\right)\left(x-4\right)\left(x-3\right)x & 0\leq x\leq 5 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.5 by means of a Fourier series of order 8.

- 1) u(1,0.5) = -17.4186
- 2) u(1,0.5) = -4.5694
- 3) u(1,0.5) = -1.27868
- 4) u(1,0.5) = -0.270107
- 5) u(1,0.5) = -2.71374

Exercise 1

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & \mathbf{0} < \mathbf{x} < \pi, \ \mathbf{0} < \mathbf{t} \\ \mathbf{u} \left(\mathbf{0}, \mathbf{t} \right) = \mathbf{u} \left(\pi, \mathbf{t} \right) = \mathbf{0} & \mathbf{0} \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \left(\mathbf{x} - \mathbf{1} \right) \ \mathbf{x} \left(\mathbf{x} - \pi \right) & \mathbf{0} \le \mathbf{x} \le \pi \\ \mathbf{0} & \mathbf{True} \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.7 by means of a Fourier series of order 12.

- 1) u(2,0.7) = -6.34781
- 2) u(2,0.7) = 6.0128
- 3) u(2,0.7) = 0.659625
- 4) u(2,0.7) = 1.94355
- 5) u(2,0.7) = -0.72533

Exercise 2

$$\begin{bmatrix} \frac{\partial^{2} u}{\partial t^{2}} (x,t) = 9 \frac{\partial^{2} u}{\partial x^{2}} (x,t) & 0 < x < 4, 0 < t \\ u (0,t) = u (4,t) = 0 & 0 \le t \\ u (x,0) = -(x-4)^{2} (x-2) x & 0 \le x \le 4 \\ \frac{\partial}{\partial t} u (x,0) = -3 (x-4)^{2} (x-3) (x-2) x^{2} & 0. \le x \le 4 \\ 0 & True \end{bmatrix}$$

Compute the position of the string at x=2 and the moment t=0.9 by means of a Fourier series of order 11.

- 1) u(2,0.9) = 1.93468
- 2) u(2,0.9) = -10.5382
- 3) u(2,0.9) = -4.9868
- 4) u(2,0.9) = -6.82367
- 5) u(2,0.9) = -5.67266

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{cases} -x & 0 \le x \le 1 \\ \frac{x}{\pi - 1} - \frac{1}{\pi - 1} - 1 & 1 \le x \le \pi \end{cases} & 0 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.6 by means of a Fourier series of order 8.

- 1) u(2,0.6) = 1.30069
- 2) u(2,0.6) = -0.377562
- 3) u(2,0.6) = -3.18347
- 4) u(2,0.6) = 2.87261
- 5) u(2,0.6) = 4.77287

Exercise 2

$$\begin{bmatrix} \frac{\partial \mathbf{u}}{\partial t} (\mathbf{x}, \mathbf{t}) = 25 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} (\mathbf{x}, \mathbf{t}) & 0 < \mathbf{x} < \mathbf{1}, \ 0 < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} (\mathbf{0}, \mathbf{t}) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} (\mathbf{1}, \mathbf{t}) = \mathbf{0} & 0 \le \mathbf{t} \\ \mathbf{u} (\mathbf{x}, \mathbf{0}) = (\mathbf{x} - \mathbf{1}) \left(\mathbf{x} - \frac{3}{5} \right) \left(\mathbf{x} - \frac{1}{5} \right) \mathbf{x} & 0 \le \mathbf{x} \le \mathbf{1} \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point $x = \frac{1}{5}$

and the moment t=0.1 by means of a Fourier series of order 8.

1)
$$u(\frac{1}{5}, 0.1) = -0.00333333$$

2)
$$u(\frac{1}{5}, 0.1) = -2.48834$$

3)
$$u(\frac{1}{5}, 0.1) = -3.55571$$

4)
$$u(\frac{1}{5}, 0.1) = 2.43829$$

5)
$$u(\frac{1}{5}, 0.1) = -0.741341$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 3, 0 < t \\ u(0,t) = u(3,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} 4x & 0 \le x \le 1 \\ 6 - 2x & 1 \le x \le 3 \end{cases} & 0 \le x \le 3 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.5 by means of a Fourier series of order 9.

- 1) u(2,0.5) = 3.25934
- 2) u(2,0.5) = 1.50469
- 3) u(2,0.5) = 5.44976
- 4) u(2,0.5) = -4.54411
- 5) u(2,0.5) = -6.56162

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t}(x,t) = 25 \frac{\partial^2 u}{\partial x^2}(x,t) & 0 < x < 2, 0 < t \\ \frac{\partial u}{\partial x}(0,t) = \frac{\partial u}{\partial x}(2,t) = 0 & 0 \le t \\ u(x,0) = \begin{bmatrix} -9x & 0 \le x \le 1 \\ 9x - 18 & 1 \le x \le 2 \end{bmatrix} & 0 \le x \le 2 \\ 0 & True \end{bmatrix}$$

Compute the temperature of the bar at the point $x = \frac{11}{10}$

and the moment t=1. by means of a Fourier series of order 10.

1)
$$u(\frac{11}{10}, 1.) = -4.5$$

2)
$$u(\frac{11}{10}, 1.) = -0.754179$$

3)
$$u(\frac{11}{10}, 1.) = 3.18552$$

4)
$$u(\frac{11}{10}, 1.) = 3.40567$$

5)
$$u(\frac{11}{10}, 1.) = 1.61686$$

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 4 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 5, \ 0 < t \\ u \left(0, t \right) = u \left(5, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = - \left(x - 5 \right)^2 \left(x - 3 \right) \left(x - 1 \right) x^2 & 0 \le x \le 5 \\ 0 & True \\ \end{bmatrix}$$

Compute the temperature of the bar at the point x=4 and the moment t=0.4 by means of a Fourier series of order 8.

- 1) u(4,0.4) = 0.397493
- 2) u(4,0.4) = -0.364002
- 3) u(4,0.4) = -1.18704
- 4) u(4,0.4) = 0.202114
- 5) u(4,0.4) = -6.01827

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 16 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (\pi,t) = 0 & 0 \le t \\ u(x,\theta) = \begin{cases} 4x & 0 \le x \le 2 \\ -\frac{8x}{\pi-2} + \frac{16}{\pi-2} + 8 & 2 \le x \le \pi \end{cases} & 0 \le x \le \pi$$

$$0 & True$$

Compute the temperature of the bar at the point x=1 and the moment t=0.4 by means of a Fourier series of order 10.

- 1) u(1,0.4) = -1.5221
- 2) u(1,0.4) = 3.9991
- 3) u(1,0.4) = 0.188309
- 4) u(1,0.4) = 1.31439
- 5) u(1,0.4) = 3.15886

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = \frac{\partial^{2}u}{\partial x^{2}}(x,t) & 0 < x < \pi, \ 0 < t \\ u(0,t) = u(\pi,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} 9x & 0 \le x \le 1 \\ 13 - 4x & 1 \le x \le 2 \\ -\frac{5x}{\pi-2} + \frac{10}{\pi-2} + 5 & 2 \le x \le \pi \end{cases} \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.6 by means of a Fourier series of order 12.

- 1) u(2,0.6) = 3.45882
- 2) u(2,0.6) = 1.95692
- 3) u(2,0.6) = -1.86238
- 4) u(2,0.6) = -0.431483
- 5) u(2,0.6) = -6.18739

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = \mathbf{16} \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 5, \ 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (5,t) = 0 & 0 \le t \\ u(x,0) = 2(x-5)^2(x-2)x & 0 \le x \le 5 \\ 0 & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=4 and the moment t=0.9 by means of a Fourier series of order 8.

- 1) u(4,0.9) = 1.90428
- 2) u(4,0.9) = 3.33649
- 3) u(4,0.9) = 0.0601037
- 4) u(4,0.9) = 0.621875
- 5) u(4,0.9) = 2.94254

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (\mathbf{x}, \mathbf{t}) = 9 \frac{\partial^2 u}{\partial x^2} (\mathbf{x}, \mathbf{t}) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ u (0, \mathbf{t}) = u (\pi, \mathbf{t}) = 0 & 0 \leq \mathbf{t} \end{cases}$$

$$\begin{cases} u (\mathbf{x}, \mathbf{0}) = \begin{cases} \frac{3x}{2} & 0 \leq x \leq 2 \\ 5 - x & 2 \leq x \leq 3 & 0 \leq x \leq \pi \\ -\frac{2x}{\pi - 3} + \frac{6}{\pi - 3} + 2 & 3 \leq x \leq \pi \end{cases}$$

$$\begin{cases} 0 & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.5 by means of a Fourier series of order 12.

- 1) u(2,0.5) = 3.79961
- 2) u(2,0.5) = 0.0265297
- 3) u(2,0.5) = -2.80178
- 4) u(2,0.5) = 8.69558
- 5) u(2,0.5) = -5.46176

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} (x,t) = 25 \frac{\partial^{2} u}{\partial x^{2}} (x,t) & 0 < x < \pi, \ 0 < t \\ u (0,t) = u (\pi,t) = 0 & 0 \le t \\ u (x,0) = 3 (x-2) x^{2} (x-\pi)^{2} & 0 \le x \le \pi \\ \frac{\partial}{\partial t} u (x,0) = 2 (x-2) x (x-\pi) & 0 \le x \le \pi \\ 0 & True \end{cases}$$

Compute the position of the string at x=2 and the moment t=0.8 by means of a Fourier series of order 8.

- 1) u(2,0.8) = 6.39862
- 2) u(2,0.8) = 1.14768
- 3) u(2,0.8) = -1.5818
- 4) u(2,0.8) = -0.00974648
- 5) u(2,0.8) = -0.848161

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 2, \ 0 < t \\ u (0,t) = u (2,t) = 0 & 0 \le t \\ u (x,0) = (x-2)^2 (x-1) x^2 & 0 \le x \le 2 \\ 0 & \text{True} \end{cases}$$

Compute the temperature of the bar at the point $x = \frac{2}{5}$

and the moment t=0.2 by means of a Fourier series of order 9.

1)
$$u(\frac{2}{5}, 0.2) = -0.0354289$$

2)
$$u(\frac{2}{5}, 0.2) = 1.40118$$

3)
$$u(\frac{2}{5}, 0.2) = 3.86831$$

4)
$$u(\frac{2}{5}, 0.2) = -3.87381$$

5)
$$u(\frac{2}{5}, 0.2) = 6.6136$$

Exercise 2

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = 25 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \mathbf{1}, \ 0 < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{1}, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = - \left(\mathbf{x} - \mathbf{1} \right)^2 \left(\mathbf{x} - \frac{\mathbf{4}}{5} \right) \mathbf{x}^2 & \mathbf{0} \le \mathbf{x} \le \mathbf{1} \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point $x = \frac{9}{10}$

and the moment t=0.4 by means of a Fourier series of order 10.

1)
$$u(\frac{9}{10}, 0.4) = 0.01$$

2)
$$u(\frac{9}{10}, 0.4) = -2.16561$$

3)
$$u(\frac{9}{10}, 0.4) = -3.82448$$

4)
$$u(\frac{9}{10}, 0.4) = -2.01629$$

5)
$$u(\frac{9}{10}, 0.4) = 2.43577$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = 9 \frac{\partial^2 u}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = 0 & 0 \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = - \left(\left(\mathbf{x} - \mathbf{3} \right) \ \mathbf{x}^2 \ \left(\mathbf{x} - \pi \right)^2 \right) & 0 \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.2 by means of a Fourier series of order 12.

- 1) u(1,0.2) = 5.2139
- 2) u(1,0.2) = 2.79533
- 3) u(1,0.2) = -1.91681
- 4) u(1,0.2) = 1.0802
- 5) u(1,0.2) = 3.85579

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = 4 \frac{\partial^2 u}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < 3, \ 0 < \mathbf{t} \\ \frac{\partial u}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial u}{\partial \mathbf{x}} \left(\mathbf{3}, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = -2 \left(\mathbf{x} - \mathbf{3} \right) \left(\mathbf{x} - \mathbf{2} \right) \mathbf{x}^2 & 0 \le \mathbf{x} \le 3 \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.5 by means of a Fourier series of order 11.

- 1) u(1,0.5) = -1.03192
- 2) u(1,0.5) = -2.36706
- 3) u(1,0.5) = 2.09834
- 4) u(1,0.5) = -3.69404
- 5) u(1,0.5) = -4.25552

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{cases} 2x & 0 \le x \le 1 \\ 8 - 6x & 1 \le x \le 2 \\ \frac{4x}{\pi - 2} - \frac{8}{\pi - 2} - 4 & 2 \le x \le \pi \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.2 by means of a Fourier series of order 12.

- 1) u(2,0.2) = -8.69998
- 2) u(2,0.2) = -1.7252
- 3) u(2,0.2) = 0.404481
- 4) u(2,0.2) = -3.81686
- 5) u(2,0.2) = -6.16587

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 4 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 4, 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (4,t) = 0 & 0 \le t \\ u(x,0) = (x-4)^2 (x-1) x & 0 \le x \le 4 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=3 and the moment t=0.1 by means of a Fourier series of order 9.

- 1) u(3,0.1) = 2.16091
- 2) u(3,0.1) = 2.38604
- 3) u(3,0.1) = -1.43399
- 4) u(3,0.1) = 4.83692
- 5) u(3,0.1) = -4.54174

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 3, \ 0 < t \\ u \left(0, t \right) = u \left(3, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \left(x - 3 \right)^2 \left(x - 2 \right) x & 0 \le x \le 3 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.9 by means of a Fourier series of order 8.

- 1) u(2,0.9) = -6.98639
- 2) u(2,0.9) = 2.76318
- 3) $u(2,0.9) = -2.9479 \times 10^{-7}$
- 4) u(2,0.9) = 6.08994
- 5) u(2,0.9) = 6.95521

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 4 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 5, \ 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (5,t) = 0 & 0 \le t \\ u(x,0) = -3 (x-5) (x-4) x & 0 \le x \le 5 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=4 and the moment t=0.7 by means of a Fourier series of order 11.

- 1) u(4,0.7) = -0.988574
- 2) u(4,0.7) = -0.874522
- 3) u(4,0.7) = 3.25174
- 4) u(4,0.7) = -14.3141
- 5) u(4,0.7) = 2.80752

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 25 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 3, \ 0 < t \\ u \left(0, t \right) = u \left(3, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = 3 \ \left(x - 3 \right) \ \left(x - 2 \right) \ \left(x - 1 \right) \ x^2 & 0 \le x \le 3 \\ 0 & True \\ \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.6 by means of a Fourier series of order 11.

- 1) u(2,0.6) = -7.17971
- 2) u(2,0.6) = 4.69937
- 3) $u(2,0.6) = -3.72405 \times 10^{-8}$
- 4) u(2,0.6) = 4.73895
- 5) u(2,0.6) = 8.21245

Exercise 2

$$\begin{cases} \frac{\partial^2 u}{\partial t^2} (x,t) = \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ u(0,t) = u(\pi,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} 4x & 0 \le x \le 2 \\ -\frac{8x}{\pi-2} + \frac{16}{\pi-2} + 8 & 2 \le x \le \pi \end{cases} & 0 \le x \le \pi \\ \frac{\partial}{\partial t} u(x,0) = \begin{cases} -3x & 0 \le x \le 1 \\ x-4 & 1 \le x \le 2 \\ \frac{2x}{\pi-2} - \frac{4}{\pi-2} - 2 & 2 \le x \le \pi \end{cases} & True$$

Compute the position of the string at x=1 and the moment t=0.9 by means of a Fourier series of order 9.

- 1) u(1,0.9) = 8.63243
- 2) u(1,0.9) = -2.21161
- 3) u(1,0.9) = 0.512164
- 4) u(1,0.9) = 2.10583
- 5) u(1,0.9) = 8.55781

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}\left(x,t\right) = 25\frac{\partial^{2}u}{\partial x^{2}}\left(x,t\right) & 0 < x < \pi, \ 0 < t \\ u\left(\theta,t\right) = u\left(\pi,t\right) = 0 & 0 \le t \\ u\left(x,\theta\right) = \begin{cases} x & 0 \le x \le 3 \\ -\frac{3x}{\pi-3} + \frac{9}{\pi-3} + 3 & 3 \le x \le \pi \end{cases} & 0 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.9 by means of a Fourier series of order 9.

- 1) u(2,0.9) = 5.38375
- 2) u(2,0.9) = 6.34046
- 3) $u(2,0.9) = 3.06661 \times 10^{-10}$
- 4) u(2,0.9) = -5.60892
- 5) u(2,0.9) = -6.77048

Exercise 2

$$\begin{bmatrix} \frac{\partial^2 u}{\partial t^2} \left(\mathbf{x}, \mathbf{t} \right) = \frac{\partial^2 u}{\partial x^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \quad 0 < \mathbf{t} \\ \mathbf{u} \left(\mathbf{0}, \mathbf{t} \right) = \mathbf{u} \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \leq \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \mathbf{2} \left(\mathbf{x} - \mathbf{2} \right) \mathbf{x} \left(\mathbf{x} - \pi \right)^2 & 0 \leq \mathbf{x} \leq \pi \\ \frac{\partial}{\partial t} \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = -\mathbf{3} \left(\mathbf{x} - \mathbf{2} \right) \left(\mathbf{x} - \mathbf{1} \right) \mathbf{x}^2 \left(\mathbf{x} - \pi \right)^2 & \mathbf{0} \cdot \leq \mathbf{x} \leq \pi \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the position of the string at x=1 and the moment t=0.6 by means of a Fourier series of order 11.

- 1) u(1,0.6) = -7.51559
- 2) u(1,0.6) = 0.722458
- 3) u(1,0.6) = 4.82793
- 4) u(1,0.6) = -6.25807
- 5) u(1,0.6) = -3.71401

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 3, \ 0 < t \\ u \left(0, t \right) = u \left(3, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = -3 \left(x - 3 \right) \left(x - 2 \right) \left(x - 1 \right) x & 0 \le x \le 3 \\ 0 & True \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.5 by means of a Fourier series of order 8.

- 1) u(2,0.5) = -7.98498
- 2) u(2,0.5) = 0.0000535456
- 3) u(2,0.5) = 3.27083
- 4) u(2,0.5) = -0.776695
- 5) u(2,0.5) = 7.76625

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} (x,t) = 16 \frac{\partial^{2} u}{\partial x^{2}} (x,t) & 0 < x < \pi, \ 0 < t \\ u (0,t) = u (\pi,t) = 0 & 0 \le t \end{cases}$$

$$\begin{cases} u (x,0) = \begin{cases} 5x & 0 \le x \le 1 \\ 6-x & 1 \le x \le 2 \\ -\frac{4x}{\pi-2} + \frac{8}{\pi-2} + 4 & 2 \le x \le \pi \end{cases}$$

$$\frac{\partial}{\partial t} u (x,0) = -2 (x-3) (x-1) x^{2} (x-\pi)^{2} 0. \le x \le \pi$$

Compute the position of the string at x=2 and the moment t=0.7 by means of a Fourier series of order 11.

- 1) u(2,0.7) = -8.08935
- 2) u(2,0.7) = -1.01037
- 3) u(2,0.7) = -2.51976
- 4) u(2,0.7) = 3.172
- 5) u(2,0.7) = -4.02781

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \end{cases}$$

$$\begin{cases} u \left(x, 0 \right) = \begin{cases} 2x & 0 \le x \le 1 \\ x+1 & 1 \le x \le 2 \\ -\frac{3x}{\pi-2} + \frac{6}{\pi-2} + 3 & 2 \le x \le \pi \end{cases}$$

$$0 & True \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.4 by means of a Fourier series of order 10.

- 1) u(2,0.4) = -4.90248
- 2) u(2,0.4) = 0.785798
- 3) u(2,0.4) = -4.46745
- 4) u(2,0.4) = 0.00398231
- 5) u(2,0.4) = -3.48701

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (\pi,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -8x & 0 \le x \le 1 \\ \frac{3x}{2} - \frac{19}{2} & 1 \le x \le 3 \\ \frac{5x}{\pi - 3} - \frac{15}{\pi - 3} - 5 & 3 \le x \le \pi \\ 0 & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.8 by means of a Fourier series of order 12.

- 1) u(2,0.8) = -3.77284
- 2) u(2,0.8) = -5.70851
- 3) u(2,0.8) = 0.85123
- 4) u(2,0.8) = -0.802205
- 5) u(2,0.8) = 3.41539

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{cases} 2x & 0 \le x \le 1 \lor 1 \le x \le 3 \\ -\frac{6x}{\pi - 3} + \frac{18}{\pi - 3} + 6 & 3 \le x \le \pi \end{cases} & 0 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.1 by means of a Fourier series of order 12.

- 1) u(2,0.1) = -8.60129
- 2) u(2,0.1) = 3.92447
- 3) u(2,0.1) = 0.904035
- 4) u(2,0.1) = -6.03704
- 5) u(2,0.1) = -4.58863

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 16 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (\pi,t) = \theta & 0 \le t \\ u(x,\theta) = \begin{cases} -\frac{2x}{3} & 0 \le x \le 3 \\ \frac{2x}{\pi-3} - \frac{6}{\pi-3} - 2 & 3 \le x \le \pi \end{cases} & 0 \le x \le \pi \end{cases}$$

$$\theta = 0 \qquad \text{True}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.9 by means of a Fourier series of order 11.

- 1) u(2,0.9) = 0.513171
- 2) u(2,0.9) = -1.
- 3) u(2,0.9) = 0.73694
- 4) u(2,0.9) = 0.361196
- 5) u(2,0.9) = -0.301549

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = 9 \frac{\partial^2 u}{\partial x^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \quad 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = 0 & 0 \leq \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = \left(\mathbf{x} - \mathbf{2} \right) \left(\mathbf{x} - \mathbf{1} \right) \mathbf{x}^2 \left(\mathbf{x} - \pi \right)^2 & 0 \leq \mathbf{x} \leq \pi \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.9 by means of a Fourier series of order 10.

- 1) u(2,0.9) = 1.19307
- 2) u(2,0.9) = 0.0000283794
- 3) u(2,0.9) = -4.23212
- 4) u(2,0.9) = -6.58303
- 5) u(2,0.9) = 5.73553

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 25 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ \theta < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (\pi,t) = \theta & 0 \le t \\ u(x,\theta) = \begin{cases} -3x & \theta \le x \le 3 \\ \frac{9x}{\pi-3} - \frac{27}{\pi-3} - 9 & 3 \le x \le \pi \end{cases} & \theta \le x \le \pi \\ \theta & True \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.7 by means of a Fourier series of order 8.

- 1) u(1,0.7) = -4.5
- 2) u(1,0.7) = -1.78784
- 3) u(1,0.7) = 1.92675
- 4) u(1,0.7) = 4.11141
- 5) u(1,0.7) = 1.12821

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 4 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 4, \quad 0 < t \\ u \left(0, t \right) = u \left(4, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = 3 \left(x - 4 \right) \left(x - 2 \right) x & 0 \le x \le 4 \\ 0 & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=3 and the moment t=0.8 by means of a Fourier series of order 12.

- 1) u(3,0.8) = -0.00345853
- 2) u(3,0.8) = 8.63728
- 3) u(3,0.8) = 2.5436
- 4) u(3,0.8) = -7.82753
- 5) u(3,0.8) = -6.23903

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 5, \ 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (5,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -\frac{7x}{2} & 0 \le x \le 2 \\ 7x - 21 & 2 \le x \le 4 \\ 35 - 7x & 4 \le x \le 5 \end{cases}$$

$$0 & True$$

Compute the temperature of the bar at the point x=4 and the moment t=0.8 by means of a Fourier series of order 11.

- 1) u(4,0.8) = 3.21493
- 2) u(4,0.8) = -1.37784
- 3) u(4,0.8) = -3.67533
- 4) u(4,0.8) = -3.95628
- 5) u(4,0.8) = 1.99294

Exercise 1

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} (\mathbf{x}, \mathbf{t}) = \mathbf{16} \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} (\mathbf{x}, \mathbf{t}) & \mathbf{0} < \mathbf{x} < \pi, \ \mathbf{0} < \mathbf{t} \\ \mathbf{u} (\mathbf{0}, \mathbf{t}) = \mathbf{u} (\pi, \mathbf{t}) = \mathbf{0} & \mathbf{0} \le \mathbf{t} \end{cases}$$

$$\begin{cases} \mathbf{u} (\mathbf{x}, \mathbf{0}) = \begin{cases} -\frac{9x}{2} & \mathbf{0} \le x \le 2 \\ 6x - 2\mathbf{1} & 2 \le x \le 3 & \mathbf{0} \le x \le \pi \\ \frac{3x}{\pi - 3} - \frac{9}{\pi - 3} - 3 & 3 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.5 by means of a Fourier series of order 11.

- 1) u(1,0.5) = -4.69705
- 2) u(1,0.5) = -0.00210093
- 3) u(1,0.5) = -1.59609
- 4) u(1,0.5) = 4.06192
- 5) u(1,0.5) = -5.77034

Exercise 2

$$\begin{bmatrix} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} (\mathbf{x}, \mathbf{t}) = 4 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} (\mathbf{x}, \mathbf{t}) & \mathbf{0} < \mathbf{x} < \pi, \ \mathbf{0} < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} (\mathbf{0}, \mathbf{t}) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} (\pi, \mathbf{t}) = \mathbf{0} & \mathbf{0} \le \mathbf{t} \\ \mathbf{u} (\mathbf{x}, \mathbf{0}) = \begin{bmatrix} -\mathbf{x} & \mathbf{0} \le \mathbf{x} \le \mathbf{1} \\ \frac{\mathbf{x}}{\pi - \mathbf{1}} - \frac{1}{\pi - \mathbf{1}} - \mathbf{1} & \mathbf{1} \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.5 by means of a Fourier series of order 8.

- 1) u(2,0.5) = 3.44042
- 2) u(2,0.5) = -1.79908
- 3) u(2,0.5) = -3.14857
- 4) u(2,0.5) = -0.490767
- 5) u(2,0.5) = -2.22539

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 9 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \quad 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \left(x - 3 \right) x^2 \left(x - \pi \right)^2 & 0 \le x \le \pi \\ 0 & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.2 by means of a Fourier series of order 9.

- 1) u(1,0.2) = -6.42008
- 2) u(1,0.2) = -4.16346
- 3) u(1,0.2) = -1.0802
- 4) u(1,0.2) = -2.85676
- 5) u(1,0.2) = 3.88189

Exercise 2

$$\begin{cases} \frac{\partial^2 u}{\partial t^2} \left(x, t \right) = 25 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = 2 \left(x - 1 \right) x \left(x - \pi \right) & 0 \le x \le \pi \\ \frac{\partial}{\partial t} u \left(x, 0 \right) = - \left(\left(x - 3 \right) \left(x - 2 \right) x \left(x - \pi \right) \right) & 0 \le x \le \pi \\ 0 & True \end{cases}$$

Compute the position of the string at x=1 and the moment t=0.1 by means of a Fourier series of order 8.

- 1) u(1,0.1) = -8.58118
- 2) u(1,0.1) = 8.51023
- 3) u(1,0.1) = 5.08149
- 4) u(1,0.1) = -3.67052
- 5) u(1,0.1) = -0.168593

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = 16 \frac{\partial^2 u}{\partial x^2}(x,t) & 0 < x < 5, 0 < t \\ u(0,t) = u(5,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -\frac{7x}{3} & 0 \le x \le 3 \\ 10x - 37 & 3 \le x \le 4 \\ 15 - 3x & 4 \le x \le 5 \end{cases} & 0 \le x \le 5 \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.4 by means of a Fourier series of order 9.

- 1) u(2,0.4) = 7.74325
- 2) u(2,0.4) = -2.47338
- 3) u(2,0.4) = 2.99043
- 4) u(2,0.4) = -0.314931
- 5) u(2,0.4) = 0.402366

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} \left(x, t \right) = \frac{\partial^{2} u}{\partial x^{2}} \left(x, t \right) & 0 < x < 2, \ 0 < t \\ u \left(0, t \right) = u \left(2, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = 3 \left(x - 2 \right)^{2} \left(x - 1 \right) x & 0 \le x \le 2 \\ \frac{\partial}{\partial t} u \left(x, 0 \right) = 2 \left(x - 2 \right) \left(x - 1 \right) x & 0 . \le x \le 2 \\ 0 & True \end{cases}$$

Compute the position of the string at $x = \frac{1}{2}$

and the moment t=1. by means of a Fourier series of order 9 .

1)
$$u(\frac{1}{2}, 1.) = -8.23831$$

2)
$$u(\frac{1}{2}, 1.) = -2.27164$$

3)
$$u(\frac{1}{2}, 1.) = 0.316559$$

4)
$$u(\frac{1}{2}, 1.) = 1.11805$$

5)
$$u(\frac{1}{2}, 1.) = -3.18075$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 25 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 2, \ 0 < t \\ u \left(0, t \right) = u \left(2, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{cases} -2 x & 0 \le x \le 1 \\ 2 x - 4 & 1 \le x \le 2 \end{cases} & 0 \le x \le 2 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point $x = \frac{3}{5}$

and the moment t=0.8 by means of a Fourier series of order 11.

1)
$$u(\frac{3}{5}, 0.8) = -2.42516$$

2)
$$u(\frac{3}{5}, 0.8) = 4.94417$$

3)
$$u(\frac{3}{5}, 0.8) = 0$$

4)
$$u(\frac{3}{5}, 0.8) = 2.51194$$

5)
$$u(\frac{3}{5}, 0.8) = -7.79399$$

Exercise 2

$$\begin{bmatrix} \frac{\partial^{2} u}{\partial t^{2}} (x,t) = 4 \frac{\partial^{2} u}{\partial x^{2}} (x,t) & 0 < x < \pi, \ 0 < t \\ u(0,t) = u(\pi,t) = 0 & 0 \le t \end{bmatrix}$$

$$\begin{bmatrix} 9 x & 0 \le x \le 1 \\ u(x,0) = \begin{cases} \frac{29}{2} - \frac{11x}{2} & 1 \le x \le 3 \\ \frac{2x}{\pi-3} - \frac{6}{\pi-3} - 2 & 3 \le x \le \pi \end{cases}$$

$$\begin{bmatrix} \frac{\partial}{\partial t} u(x,0) = \begin{cases} 8x & 0 \le x \le 1 \\ -\frac{8x}{\pi-1} + \frac{8}{\pi-1} + 8 & 1 \le x \le \pi \end{cases}$$

$$0 \le x \le \pi$$

$$\begin{bmatrix} \frac{\partial}{\partial t} u(x,0) = \begin{cases} -\frac{8x}{\pi-1} + \frac{8}{\pi-1} + 8 & 1 \le x \le \pi \end{cases}$$
True

Compute the position of the string at x=2

and the moment t=0.1 by means of a Fourier series of order 10.

1)
$$u(2,0.1) = 0.52199$$

2)
$$u(2,0.1) = -6.99105$$

3)
$$u(2,0.1) = 3.89733$$

4)
$$u(2,0.1) = -3.95571$$

5)
$$u(2,0.1) = -8.00811$$

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ u(0,t) = u(\pi,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} 3x & 0 \le x \le 2 \\ 16 - 5x & 2 \le x \le 3 \\ -\frac{x}{\pi - 3} + \frac{3}{\pi - 3} + 1 & 3 \le x \le \pi \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.7 by means of a Fourier series of order 10.

1)
$$u(1,0.7) = 7.87936$$

2)
$$u(1,0.7) = 8.13818$$

3)
$$u(1,0.7) = 1.95417$$

4)
$$u(1,0.7) = -2.69203$$

5)
$$u(1,0.7) = 7.00648$$

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = 25 \frac{\partial^2 u}{\partial x^2}(x,t) & 0 < x < 1, 0 < t \\ \frac{\partial u}{\partial x}(0,t) = \frac{\partial u}{\partial x}(1,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} 45 & x & 0 \le x \le \frac{1}{5} \\ \frac{43}{3} - \frac{80 x}{3} & \frac{1}{5} \le x \le \frac{1}{2} & 0 \le x \le 1 \\ 2 - 2 & x & \frac{1}{2} \le x \le 1 \end{cases}$$

Compute the temperature of the bar at the point $x = \frac{3}{10}$

and the moment t=0.7 by means of a Fourier series of order 10.

1)
$$u(\frac{3}{10}, 0.7) = -4.49502$$

2)
$$u(\frac{3}{10}, 0.7) = -0.374754$$

3)
$$u(\frac{3}{10}, 0.7) = -0.166826$$

4)
$$u(\frac{3}{10}, 0.7) = 2.65$$

5)
$$u(\frac{3}{10}, 0.7) = 1.18252$$

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = 9 \frac{\partial^2 u}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \quad 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = 2 \left(\mathbf{x} - \mathbf{2} \right) \left(\mathbf{x} - \mathbf{1} \right) \mathbf{x} \left(\mathbf{x} - \pi \right) & 0 \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.4 by means of a Fourier series of order 12.

- 1) u(1,0.4) = -3.12051
- 2) u(1,0.4) = 0.763494
- 3) u(1,0.4) = 8.53863
- 4) u(1,0.4) = -0.0107749
- 5) u(1,0.4) = -3.87606

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 9 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 2, 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (2,t) = 0 & 0 \le t \\ u(x,0) = \begin{bmatrix} -8 & 0 \le x \le 1 \\ 8 & x - 16 & 1 \le x \le 2 \end{bmatrix} & 0 \le x \le 2 \\ 0 & True \end{bmatrix}$$

Compute the temperature of the bar at the point $x = \frac{9}{10}$

and the moment t=0.9 by means of a Fourier series of order 10.

1)
$$u(\frac{9}{10}, 0.9) = 0.869488$$

2)
$$u(\frac{9}{10}, 0.9) = 3.72622$$

3)
$$u(\frac{9}{10}, 0.9) = 0.889709$$

4)
$$u(\frac{9}{10}, 0.9) = -4.$$

5)
$$u(\frac{9}{10}, 0.9) = -3.25008$$

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 4 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = - \left(\left(x - 3 \right) \left(x - 2 \right) \right. \left. x^2 \left(x - \pi \right) \right) & 0 \le x \le \pi \\ 0 & True \\ \end{bmatrix}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.8 by means of a Fourier series of order 8.

- 1) u(1,0.8) = 0.0757015
- 2) u(1,0.8) = -2.57685
- 3) u(1,0.8) = 3.68338
- 4) u(1,0.8) = -2.71338
- 5) u(1,0.8) = -2.88226

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 9 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 1, 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (1,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} \frac{2\theta x}{3} & 0 \le x \le \frac{3}{5} \\ 10 - 10 x & \frac{3}{5} \le x \le 1 \end{cases} & 0 \le x \le 1 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point $x = \frac{4}{5}$

and the moment t=0.4 by means of a Fourier series of order 8.

1)
$$u(\frac{4}{5}, 0.4) = 1.45991$$

2)
$$u(\frac{4}{5}, 0.4) = -4.1035$$

3)
$$u(\frac{4}{5}, 0.4) = -0.870065$$

4)
$$u(\frac{4}{5}, 0.4) = 2.$$

5)
$$u(\frac{4}{5}, 0.4) = 0.449094$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 4 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 5, \ 0 < t \\ u \left(\theta, t \right) = u \left(5, t \right) = 0 & \theta \le t \\ u \left(x, \theta \right) = \begin{cases} -x & \theta \le x \le 3 \\ 12 \ x - 39 & 3 \le x \le 4 \\ 45 - 9 \ x & 4 \le x \le 5 \end{cases} \\ \theta & True \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.8 by means of a Fourier series of order 8.

- 1) u(1,0.8) = -4.79162
- 2) u(1,0.8) = -3.59116
- 3) u(1,0.8) = -0.0223525
- 4) u(1,0.8) = 8.1424
- 5) u(1,0.8) = -4.20647

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 9 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (\pi,t) = \theta & 0 \le t \\ u(x,\theta) = \begin{cases} -2x & \theta \le x \le 2 \\ \frac{4x}{\pi-2} - \frac{8}{\pi-2} - 4 & 2 \le x \le \pi \end{cases} & 0 \le x \le \pi \end{cases}$$

$$\theta = 0 \qquad \text{True}$$

Compute the temperature of the bar at the point x=1 and the moment t=1. by means of a Fourier series of order 9.

- 1) u(1,1) = -1.20434
- 2) u(1,1) = 4.54249
- 3) u(1,1) = -1.99997
- 4) u(1,1) = -2.59451
- 5) u(1,1) = 3.88692

Exercise 1

```
 \begin{bmatrix} \frac{\partial u}{\partial t} \left( \mathbf{X}, \mathbf{t} \right) = 9 \frac{\partial^2 u}{\partial x^2} \left( \mathbf{X}, \mathbf{t} \right) & 0 < \mathbf{X} < \pi, \quad 0 < \mathbf{t} \\ u \left( \mathbf{0}, \mathbf{t} \right) = u \left( \pi, \mathbf{t} \right) = 0 & 0 \le \mathbf{t} \\ u \left( \mathbf{X}, \mathbf{0} \right) = -3 \left( \mathbf{X} - \mathbf{1} \right) \mathbf{X} \left( \mathbf{X} - \pi \right)^2 & 0 \le \mathbf{X} \le \pi \\ \mathbf{0} & \text{True}
```

Compute the temperature of the bar at the point x=2 and the moment t=0.5 by means of a Fourier series of order 12.

- 1) u(2,0.5) = -0.0431837
- 2) u(2,0.5) = -7.67777
- 3) u(2,0.5) = -1.07085
- 4) u(2,0.5) = 0.523571
- 5) u(2,0.5) = 3.43892

Exercise 2

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} (\mathbf{x}, \mathbf{t}) = 9 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} (\mathbf{x}, \mathbf{t}) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} (\mathbf{0}, \mathbf{t}) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} (\pi, \mathbf{t}) = \mathbf{0} & 0 \le \mathbf{t} \\ \mathbf{u} (\mathbf{x}, \mathbf{0}) = 3 (\mathbf{x} - \mathbf{1}) \mathbf{x} (\mathbf{x} - \pi) & 0 \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.1 by means of a Fourier series of order 9.

- 1) u(1,0.1) = -1.18235
- 2) u(1,0.1) = -1.94191
- 3) u(1,0.1) = 0.426529
- 4) u(1,0.1) = -3.99964
- 5) u(1,0.1) = 2.86089

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = 4\frac{\partial^2 u}{\partial x^2}(x,t) & 0 < x < 3, 0 < t \\ u(0,t) = u(3,t) = 0 & 0 \le t \\ u(x,0) = 2(x-3)^2(x-1)x & 0 \le x \le 3 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=1. by means of a Fourier series of order 12.

- 1) u(1,1.) = 8.12156
- 2) u(1,1) = -5.77859
- 3) u(1,1) = 1.7678
- 4) u(1,1) = 0.022157
- 5) u(1,1) = 6.50802

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = 9 \frac{\partial^2 u}{\partial x^2}(x,t) & 0 < x < 1, 0 < t \\ \frac{\partial u}{\partial x}(0,t) = \frac{\partial u}{\partial x}(1,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -15 x & 0 \le x \le \frac{1}{5} \\ -2 x - \frac{13}{5} & \frac{1}{5} \le x \le \frac{7}{10} & 0 \le x \le 1 \\ \frac{40 x}{3} - \frac{40}{3} & \frac{7}{10} \le x \le 1 \end{cases}$$

Compute the temperature of the bar at the point $x = \frac{9}{10}$

and the moment t=0.3 by means of a Fourier series of order 8.

1)
$$u(\frac{9}{10}, 0.3) = -3.53464$$

2)
$$u(\frac{9}{10}, 0.3) = -4.20875$$

3)
$$u(\frac{9}{10}, 0.3) = -2.65$$

4)
$$u(\frac{9}{10}, 0.3) = -4.3672$$

5)
$$u\left(\frac{9}{10}, 0.3\right) = 0.489876$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = 4\frac{\partial^{2}u}{\partial x^{2}}(x,t) & 0 < x < 1, \ 0 < t \\ u(0,t) = u(1,t) = 0 & 0 \le t \end{cases}$$

$$\begin{cases} u(x,0) = \begin{cases} 5x & 0 \le x \le \frac{2}{5} \\ 8 - 15x & \frac{2}{5} \le x \le \frac{3}{5} & 0 \le x \le 1 \\ \frac{5x}{2} - \frac{5}{2} & \frac{3}{5} \le x \le 1 \end{cases}$$

$$0 & True$$

Compute the temperature of the bar at the point $x = \frac{1}{2}$

and the moment t=1. by means of a Fourier series of order 9.

1)
$$u(\frac{1}{2}, 1.) = 3.14028$$

2)
$$u(\frac{1}{2}, 1.) = 0$$

3)
$$u(\frac{1}{2}, 1.) = -1.04315$$

4)
$$u(\frac{1}{2}, 1.) = -6.57169$$

5)
$$u(\frac{1}{2}, 1.) = -1.46949$$

Exercise 2

$$\begin{cases} \frac{\partial^2 u}{\partial t^2} \left(\mathbf{X}, \mathbf{t} \right) = \frac{\partial^2 u}{\partial x^2} \left(\mathbf{X}, \mathbf{t} \right) & 0 < \mathbf{X} < \pi, \ 0 < \mathbf{t} \\ \mathbf{u} \left(\mathbf{0}, \mathbf{t} \right) = \mathbf{u} \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \leq \mathbf{t} \\ \mathbf{u} \left(\mathbf{X}, \mathbf{0} \right) = \begin{cases} -\frac{9 \, x}{2} & 0 \leq \mathbf{X} \leq \mathbf{2} \\ \frac{9 \, x}{\pi - 2} - \frac{18}{\pi - 2} - 9 & 2 \leq \mathbf{X} \leq \pi \end{cases} & 0 \leq \mathbf{X} \leq \pi \\ \frac{\partial}{\partial t} \mathbf{u} \left(\mathbf{X}, \mathbf{0} \right) = -3 \left(\mathbf{X} - \mathbf{2} \right) \left(\mathbf{X} - \mathbf{1} \right) \mathbf{X}^2 \left(\mathbf{X} - \pi \right) & \mathbf{0} \cdot \leq \mathbf{X} \leq \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the position of the string at x=2 and the moment t=0.4 by means of a Fourier series of order 10.

- 1) u(2,0.4) = -6.15006
- 2) u(2,0.4) = -0.976704
- 3) u(2,0.4) = -1.67132
- 4) u(2,0.4) = -3.78573
- 5) u(2,0.4) = -1.16547

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 9 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 3, \ 0 < t \\ u (0,t) = u (3,t) = 0 & 0 \le t \\ u (x,0) = -3 (x-3) (x-2) (x-1) x & 0 \le x \le 3 \\ 0 & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.7 by means of a Fourier series of order 9.

- 1) u(2,0.7) = -8.53381
- 2) u(2,0.7) = 3.72816
- 3) u(2,0.7) = 1.20171
- 4) u(2,0.7) = -2.83121
- 5) u(2,0.7) = 0.000345431

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} \left(\mathbf{x}, \mathbf{t} \right) = 4 \frac{\partial^{2} u}{\partial x^{2}} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = - \left(\left(\mathbf{x} - \mathbf{3} \right) \left(\mathbf{x} - \mathbf{2} \right) \mathbf{x} \left(\mathbf{x} - \pi \right)^{2} \right) & 0 \le \mathbf{x} \le \pi \\ \frac{\partial}{\partial t} u \left(\mathbf{x}, \mathbf{0} \right) = \left(\mathbf{x} - \mathbf{3} \right) \left(\mathbf{x} - \mathbf{2} \right) \mathbf{x}^{2} \left(\mathbf{x} - \pi \right)^{2} & \mathbf{0} . \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the position of the string at x=2 and the moment t=0.1 by means of a Fourier series of order 12.

- 1) u(2,0.1) = -6.61544
- 2) u(2,0.1) = -0.246878
- 3) u(2,0.1) = -2.66146
- 4) u(2,0.1) = 4.53216
- 5) u(2,0.1) = 5.48524

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = - \left(\left(x - 3 \right) \right. \left(x - 2 \right) \left. x \left(x - \pi \right) \right. \right) & 0 \le x \le \pi \\ 0 & True \\ \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.8 by means of a Fourier series of order 12.

- 1) u(2,0.8) = -4.99606
- 2) u(2,0.8) = -7.17203
- 3) u(2,0.8) = 0.902623
- 4) u(2,0.8) = 1.64076
- 5) u(2,0.8) = -0.498036

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 25 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (\pi,t) = \theta & 0 \le t \\ u(x,\theta) = \begin{cases} -\frac{3x}{2} & 0 \le x \le 2 \\ 3 - 3x & 2 \le x \le 3 & 0 \le x \le \pi \\ \frac{6x}{\pi - 3} - \frac{18}{\pi - 3} - 6 & 3 \le x \le \pi \end{cases}$$

$$\theta = 0 \qquad \qquad \text{True}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.1 by means of a Fourier series of order 9.

- 1) u(2,0.1) = 1.17119
- 2) u(2,0.1) = 4.28943
- 3) u(2,0.1) = 1.22894
- 4) u(2,0.1) = -2.59694
- 5) u(2,0.1) = 0.434243

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = \mathbf{16} \frac{\partial^2 u}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & \mathbf{0} < \mathbf{x} < \pi, \quad \mathbf{0} < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = \mathbf{0} & \mathbf{0} \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = -3 \left(\mathbf{x} - \mathbf{3} \right) \mathbf{x} \left(\mathbf{x} - \pi \right) & \mathbf{0} \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.1 by means of a Fourier series of order 8.

- 1) u(2,0.1) = -1.99877
- 2) u(2,0.1) = 1.01185
- 3) u(2,0.1) = 3.04341
- 4) u(2,0.1) = 3.58106
- 5) u(2,0.1) = -7.65367

Exercise 2

$$\begin{cases} \frac{\partial^2 u}{\partial t^2} \left(\mathbf{x}, \mathbf{t} \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ \mathbf{u} \left(\mathbf{0}, \mathbf{t} \right) = \mathbf{u} \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \begin{cases} -\mathbf{x} & 0 \le \mathbf{x} \le \mathbf{1} \\ 3 - 4 \mathbf{x} & 1 \le \mathbf{x} \le \mathbf{3} \\ \frac{9 \mathbf{x}}{\pi - \mathbf{3}} - \frac{27}{\pi - \mathbf{3}} - 9 & 3 \le \mathbf{x} \le \pi \end{cases} \\ \frac{\partial}{\partial t} \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \mathbf{2} \left(\mathbf{x} - \mathbf{1} \right) \mathbf{x} \left(\mathbf{x} - \pi \right) & \mathbf{0} \cdot \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the position of the string at x=2 and the moment t=1. by means of a Fourier series of order 9.

- 1) u(2,1.) = 6.06678
- 2) u(2,1) = 2.95967
- 3) u(2,1) = -6.36303
- 4) u(2,1) = -8.37912
- 5) u(2,1) = 4.97899

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 16 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ u(0,t) = u(\pi,t) = 0 & 0 \le t \end{cases}$$

$$\begin{cases} u(x,0) = \begin{cases} -6x & 0 \le x \le 1 \\ -\frac{3x}{2} - \frac{9}{2} & 1 \le x \le 3 \\ \frac{9x}{\pi - 3} - \frac{27}{\pi - 3} - 9 & 3 \le x \le \pi \end{cases}$$

$$\begin{cases} 0 & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.8 by means of a Fourier series of order 8.

- 1) u(1,0.8) = -0.0000191792
- 2) u(1,0.8) = -6.11255
- 3) u(1,0.8) = 1.76734
- 4) u(1,0.8) = -6.42418
- 5) u(1,0.8) = 2.48023

Exercise 2

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = 4 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \mathbf{5}, \ 0 < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{5}, \mathbf{t} \right) = \mathbf{0} & 0 \leq \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \left(\mathbf{x} - \mathbf{5} \right) \ \left(\mathbf{x} - \mathbf{2} \right) \ \left(\mathbf{x} - \mathbf{1} \right) \ \mathbf{x}^2 & \mathbf{0} \leq \mathbf{x} \leq \mathbf{5} \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=4 and the moment t=0.3 by means of a Fourier series of order 10.

- 1) u(4,0.3) = 3.17182
- 2) u(4,0.3) = -4.8595
- 3) u(4,0.3) = -3.19897
- 4) u(4,0.3) = -54.6062
- 5) u(4,0.3) = -0.412566

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = 4\frac{\partial^{2}u}{\partial x^{2}}(x,t) & 0 < x < 1, \ 0 < t \\ u(0,t) = u(1,t) = 0 & 0 \le t \end{cases}$$

$$\begin{cases} u(x,0) = \begin{cases} -50 \ x & 0 \le x \le \frac{1}{10} \\ \frac{80 \ x}{7} - \frac{43}{7} & \frac{1}{10} \le x \le \frac{4}{5} & 0 \le x \le 1 \\ 15 - 15 \ x & \frac{4}{5} \le x \le 1 \end{cases}$$

Compute the temperature of the bar at the point $x = \begin{array}{c} 1 \\ - \\ 2 \end{array}$

and the moment t=0.9 by means of a Fourier series of order 10.

1)
$$u(\frac{1}{2}, 0.9) = -2.52388$$

2)
$$u(\frac{1}{2}, 0.9) = 8.74082$$

3)
$$u(\frac{1}{2}, 0.9) = -7.49603$$

4)
$$u(\frac{1}{2}, 0.9) = -4.68405$$

5)
$$u(\frac{1}{2}, 0.9) = 0$$

Exercise 2

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = \mathbf{16} \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & \mathbf{0} < \mathbf{x} < \pi, \quad \mathbf{0} < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\pi, \mathbf{t} \right) = \mathbf{0} & \mathbf{0} \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \mathbf{3} \left(\mathbf{x} - \mathbf{3} \right) \, \mathbf{x}^2 \, \left(\mathbf{x} - \pi \right)^2 & \mathbf{0} \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=1. by means of a Fourier series of order 10.

- 1) u(1,1) = -13.9217
- 2) u(1,1) = -1.36216
- 3) u(1,1) = 2.53052
- 4) u(1,1) = -0.338906
- 5) u(1,1) = 2.04126

Exercise 1

$$\begin{bmatrix} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = 9 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \quad 0 < \mathbf{t} \\ \mathbf{u} \left(\mathbf{0}, \mathbf{t} \right) = \mathbf{u} \left(\pi, \mathbf{t} \right) = 0 & 0 \leq \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = -2 \left(\mathbf{x} - 2 \right) \left(\mathbf{x} - \mathbf{1} \right) \mathbf{x} \left(\mathbf{x} - \pi \right)^2 & 0 \leq \mathbf{x} \leq \pi \\ \mathbf{0} & \text{True} \\ \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.4 by means of a Fourier series of order 11.

- 1) u(2,0.4) = 6.49287
- 2) u(2,0.4) = 2.35034
- 3) u(2,0.4) = 7.39726
- 4) u(2,0.4) = -0.0122513
- 5) u(2,0.4) = -4.0516

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 16 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (\pi,t) = 0 & 0 \le t \\ u(x,0) = \begin{bmatrix} -x & 0 \le x \le 1 \\ 6x - 7 & 1 \le x \le 2 \\ -\frac{5x}{\pi - 2} + \frac{10}{\pi - 2} + 5 & 2 \le x \le \pi \end{bmatrix}$$

$$0 \text{ True}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.8 by means of a Fourier series of order 9.

- 1) u(1,0.8) = 2.39092
- 2) u(1,0.8) = 1.38591
- 3) u(1,0.8) = -2.50913
- 4) u(1,0.8) = -2.24078
- 5) u(1,0.8) = -0.227812

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 4 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 5, \ 0 < t \\ u(0,t) = u(5,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} \frac{9x}{2} & 0 \le x \le 2 \\ 25 - 8x & 2 \le x \le 3 & 0 \le x \le 5 \\ \frac{5}{2} - \frac{x}{2} & 3 \le x \le 5 \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.5 by means of a Fourier series of order 9.

- 1) u(1,0.5) = -0.0425985
- 2) u(1,0.5) = 7.75696
- 3) u(1,0.5) = 1.40595
- 4) u(1,0.5) = 7.51006
- 5) u(1,0.5) = -0.708462

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} (x,t) = \frac{\partial^{2} u}{\partial x^{2}} (x,t) & 0 < x < \pi, \ 0 < t \\ u (0,t) = u (\pi,t) = 0 & 0 \le t \\ u (x,0) = (x-3) (x-1) x (x-\pi)^{2} & 0 \le x \le \pi \\ \frac{\partial}{\partial t} u (x,0) = 3 (x-2) (x-1) x^{2} (x-\pi) & 0 \le x \le \pi \\ 0 & \text{True} \end{cases}$$

Compute the position of the string at x=2 and the moment t=0.4 by means of a Fourier series of order 11.

- 1) u(2,0.4) = 1.58969
- 2) u(2,0.4) = 3.08413
- 3) u(2,0.4) = 2.95909
- 4) u(2,0.4) = -3.44099
- 5) u(2,0.4) = -2.47032

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = \frac{\partial^2 u}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \leq \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = 3 \left(\mathbf{x} - 3 \right) \ \mathbf{x}^2 \left(\mathbf{x} - \pi \right)^2 & 0 \leq \mathbf{x} \leq \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.5 by means of a Fourier series of order 9.

- 1) u(2,0.5) = 8.6125
- 2) u(2,0.5) = -12.0506
- 3) u(2,0.5) = -5.97823
- 4) u(2,0.5) = -3.21786
- 5) u(2,0.5) = 8.94394

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 9 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 5, 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (5,t) = \theta & 0 \le t \\ u(x,0) = \begin{cases} x & 0 \le x \le 2 \\ 2x - 2 & 2 \le x \le 4 & 0 \le x \le 5 \\ 30 - 6x & 4 \le x \le 5 \end{cases} \\ \theta & True \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.2 by means of a Fourier series of order 9.

- 1) u(2,0.2) = -1.90858
- 2) u(2,0.2) = -3.30943
- 3) u(2,0.2) = -1.46217
- 4) u(2,0.2) = 2.36914
- 5) u(2,0.2) = -4.9711

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 4 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 1, 0 < t \\ u(0,t) = u(1,t) = 0 & 0 \le t \\ u(x,0) = (x-1) \left(x - \frac{3}{10}\right) x & 0 \le x \le 1 \\ 0 & True \end{bmatrix}$$

Compute the temperature of the bar at the point $x = \frac{3}{10}$

and the moment t=0.8 by means of a Fourier series of order 8.

1)
$$u(\frac{3}{10}, 0.8) = 3.89953$$

2)
$$u(\frac{3}{10}, 0.8) = -2.17683$$

3)
$$u(\frac{3}{10}, 0.8) = 0$$

4)
$$u(\frac{3}{10}, 0.8) = 6.50652$$

5)
$$u\left(\frac{3}{10}, 0.8\right) = -1.61036$$

Exercise 2

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = \mathbf{16} \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = -\mathbf{2} \left(\mathbf{x} - \mathbf{3} \right) \ \mathbf{x}^2 \left(\mathbf{x} - \pi \right)^2 & 0 \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.2 by means of a Fourier series of order 12.

- 1) u(2,0.2) = 4.16656
- 2) u(2,0.2) = -4.02223
- 3) u(2,0.2) = -0.0959473
- 4) u(2,0.2) = 9.21359
- 5) u(2,0.2) = 3.43348

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 2, \ 0 < t \\ u \left(0, t \right) = u \left(2, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{cases} 7x & 0 \le x \le 1 \\ 14 - 7x & 1 \le x \le 2 \end{cases} & 0 \le x \le 2 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point $x = \frac{3}{5}$

and the moment t=0.8 by means of a Fourier series of order 8.

1)
$$u(\frac{3}{5}, 0.8) = -6.90286$$

2)
$$u(\frac{3}{5}, 0.8) = 0.637651$$

3)
$$u(\frac{3}{5}, 0.8) = -8.41964$$

4)
$$u(\frac{3}{5}, 0.8) = 6.78643$$

5)
$$u(\frac{3}{5}, 0.8) = 3.46507$$

Exercise 2

$$\begin{bmatrix} \frac{\partial \mathbf{u}}{\partial t} (\mathbf{x}, \mathbf{t}) = 4 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} (\mathbf{x}, \mathbf{t}) & 0 < \mathbf{x} < \mathbf{5}, \ 0 < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} (\mathbf{0}, \mathbf{t}) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} (\mathbf{5}, \mathbf{t}) = \mathbf{0} & 0 \le \mathbf{t} \\ \mathbf{u} (\mathbf{x}, \mathbf{0}) = -(\mathbf{x} - \mathbf{5})^2 (\mathbf{x} - \mathbf{2}) \mathbf{x}^2 & 0 \le \mathbf{x} \le \mathbf{5} \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.9 by means of a Fourier series of order 8.

- 1) u(1,0.9) = -6.43296
- 2) u(1,0.9) = 0.196649
- 3) u(1,0.9) = -2.91887
- 4) u(1,0.9) = -2.5097
- 5) u(1,0.9) = -3.80573

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 25 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ u(0,t) = u(\pi,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -3x & 0 \le x \le 2 \\ 5x - 16 & 2 \le x \le 3 \\ \frac{x}{\pi - 3} - \frac{3}{\pi - 3} - 1 & 3 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.7 by means of a Fourier series of order 11.

- 1) u(2,0.7) = 3.57059
- 2) u(2,0.7) = 8.86103
- 3) u(2,0.7) = 3.18862
- 4) u(2,0.7) = 4.24979
- 5) $u(2,0.7) = -1.09968 \times 10^{-7}$

Exercise 2

$$\begin{cases} \frac{\partial^2 u}{\partial t^2} \left(\mathbf{x}, \mathbf{t} \right) = \frac{\partial^2 u}{\partial x^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = 3 & \left(\mathbf{x} - 2 \right) & \left(\mathbf{x} - 1 \right) & \mathbf{x}^2 & \left(\mathbf{x} - \pi \right) & 0 \le \mathbf{x} \le \pi \\ \frac{\partial}{\partial t} u \left(\mathbf{x}, \mathbf{0} \right) = \begin{cases} \frac{3x}{2} & 0 \le x \le 2 \\ 25 - 11x & 2 \le x \le 3 & 0. \le \mathbf{x} \le \pi \\ \frac{8x}{\pi - 3} - \frac{24}{\pi - 3} - 8 & 3 \le x \le \pi \end{cases}$$

$$\begin{cases} \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{cases}$$
True

Compute the position of the string at x=1 and the moment t=0.8 by means of a Fourier series of order 11.

- 1) u(1,0.8) = -1.83393
- 2) u(1,0.8) = -3.89148
- 3) u(1,0.8) = 6.30202
- 4) u(1,0.8) = 8.99529
- 5) u(1,0.8) = 1.92669

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 25 \frac{\partial^2 u}{\partial x^2} (x,t) & \theta < x < \pi, \ \theta < t \\ u (\theta,t) = u (\pi,t) = \theta & \theta \le t \end{cases}$$

$$\begin{cases} u (x,\theta) = \begin{cases} -8x & \theta \le x \le 1 \\ \frac{x}{2} - \frac{17}{2} & 1 \le x \le 3 \\ \frac{7x}{\pi - 3} - \frac{21}{\pi - 3} - 7 & 3 \le x \le \pi \end{cases}$$

$$\begin{cases} \theta & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.2 by means of a Fourier series of order 12.

1) u(1,0.2) = -0.0507444

2) u(1,0.2) = -3.36009

3) u(1,0.2) = 3.2086

4) u(1,0.2) = 1.7687

5) u(1,0.2) = 8.73948

Exercise 2

$$\begin{cases} \frac{\partial^2 u}{\partial t^2} \left(\mathbf{x}, \mathbf{t} \right) = 9 \frac{\partial^2 u}{\partial x^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = 0 & 0 \leq \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = 2 \left(\mathbf{x} - \mathbf{1} \right) \mathbf{x}^2 \left(\mathbf{x} - \pi \right)^2 & 0 \leq \mathbf{x} \leq \pi \\ \frac{\partial}{\partial t} u \left(\mathbf{x}, \mathbf{0} \right) = \begin{cases} -\frac{7x}{3} & 0 \leq \mathbf{x} \leq 3 \\ \frac{7x}{\pi - 3} - \frac{21}{\pi - 3} - 7 & 3 \leq \mathbf{x} \leq \pi \end{cases} & \mathbf{0}. \leq \mathbf{x} \leq \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the position of the string at x=1 and the moment t=1. by means of a Fourier series of order 11.

1) u(1,1) = 5.69043

2) u(1,1) = -10.3719

3) u(1,1) = 6.81015

4) u(1,1) = -7.04813

5) u(1,1) = -3.28024

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 25 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{cases} \frac{4x}{3} & 0 \le x \le 3 \\ -\frac{4x}{\pi - 3} + \frac{12}{\pi - 3} + 4 & 3 \le x \le \pi \end{cases} & 0 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.1 by means of a Fourier series of order 9.

- 1) u(1,0.1) = 7.64682
- 2) u(1,0.1) = -6.86544
- 3) u(1,0.1) = 3.43608
- 4) u(1,0.1) = 0.183523
- 5) u(1,0.1) = -7.57748

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}}(x,t) = 4 \frac{\partial^{2} u}{\partial x^{2}}(x,t) & 0 < x < 1, \ 0 < t \\ u(0,t) = u(1,t) = 0 & 0 \le t \\ u(x,0) = 2(x-1)(x-\frac{2}{5})x^{2} & 0 \le x \le 1 \end{cases}$$

$$\begin{cases} \frac{\partial}{\partial t} u(x,0) = \begin{cases} -20x & 0 \le x \le \frac{2}{5} \\ -5x-6 & \frac{2}{5} \le x \le \frac{3}{5} \end{cases} & 0. \le x \le 1 \end{cases}$$

Compute the position of the string at $x = \frac{3}{5}$

and the moment t=0.7 by means of a Fourier series of order 9.

1)
$$u(\frac{3}{5}, 0.7) = 6.67817$$

2)
$$u(\frac{3}{5}, 0.7) = -3.23076$$

3)
$$u(\frac{3}{5}, 0.7) = 3.86326$$

4)
$$u(\frac{3}{5}, 0.7) = 1.21259$$

5)
$$u(\frac{3}{5}, 0.7) = -1.63782$$

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(\mathbf{X}, \mathbf{t} \right) = \mathbf{16} \frac{\partial^2 u}{\partial x^2} \left(\mathbf{X}, \mathbf{t} \right) & 0 < \mathbf{x} < \mathbf{2}, \ 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\mathbf{2}, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = \begin{bmatrix} -x & 0 \le x \le \mathbf{1} \\ x - 2 & \mathbf{1} \le x \le \mathbf{2} \end{bmatrix} & 0 \le x \le \mathbf{2} \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point $x = \frac{8}{5}$

and the moment t=0.8 by means of a Fourier series of order 8.

1)
$$u(\frac{8}{5}, 0.8) = -1.04073$$

2)
$$u(\frac{8}{5}, 0.8) = -6.89141$$

3)
$$u(\frac{8}{5}, 0.8) = 8.42786$$

4)
$$u(\frac{8}{5}, 0.8) = 0.896257$$

5)
$$u(\frac{8}{5}, 0.8) = 0$$

Exercise 2

$$\begin{cases} \frac{\partial^{2}u}{\partial t^{2}}\left(x,t\right)=25\frac{\partial^{2}u}{\partial x^{2}}\left(x,t\right) & 0< x< 5, \ 0< t \\ u\left(0,t\right)=u\left(5,t\right)=0 & 0\leq t \\ u\left(x,0\right)=2\left(x-5\right)^{2}\left(x-4\right)\left(x-2\right)x^{2} & 0\leq x\leq 5 \\ \frac{\partial}{\partial t}u\left(x,0\right)=\begin{cases} \frac{x}{4} & 0\leq x\leq 4 \\ 5-x & 4\leq x\leq 5 \end{cases} & 0.\leq x\leq 5 \\ 0 & \text{True} \end{cases}$$

Compute the position of the string at x=3 and the moment t=0.1 by means of a Fourier series of order 8.

- 1) u(3,0.1) = 2.8741
- 2) u(3,0.1) = -48.8205
- 3) u(3,0.1) = 1.16098
- 4) u(3,0.1) = 3.08688
- 5) u(3,0.1) = 0.775257

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 9 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \quad 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = 2 \left(x - 3 \right) \left(x - 1 \right) x \left(x - \pi \right)^2 & 0 \le x \le \pi \\ 0 & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.8 by means of a Fourier series of order 11.

- 1) u(1,0.8) = -0.747062
- 2) u(1,0.8) = -0.00148067
- 3) u(1,0.8) = -7.38947
- 4) u(1,0.8) = 6.69706
- 5) u(1,0.8) = -4.03281

Exercise 2

$$\begin{bmatrix} \frac{\partial^2 u}{\partial t^2} \left(\mathbf{X}, \mathbf{t} \right) = \frac{\partial^2 u}{\partial x^2} \left(\mathbf{X}, \mathbf{t} \right) & 0 < \mathbf{X} < \pi, \ 0 < \mathbf{t} \\ \mathbf{u} \left(\mathbf{0}, \mathbf{t} \right) = \mathbf{u} \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \leq \mathbf{t} \\ \mathbf{u} \left(\mathbf{X}, \mathbf{0} \right) = \begin{cases} \frac{x}{2} & 0 \leq \mathbf{X} \leq \mathbf{2} \\ -\frac{x}{\pi - 2} + \frac{2}{\pi - 2} + \mathbf{1} & 2 \leq \mathbf{X} \leq \pi \end{cases} & 0 \leq \mathbf{X} \leq \pi \\ \frac{\partial}{\partial t} \mathbf{u} \left(\mathbf{X}, \mathbf{0} \right) = \begin{cases} -4 & 0 \leq \mathbf{X} \leq \mathbf{2} \\ \frac{8x}{\pi - 2} - \frac{16}{\pi - 2} - \mathbf{8} & 2 \leq \mathbf{X} \leq \pi \end{cases} & \mathbf{0} \cdot \leq \mathbf{X} \leq \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the position of the string at x=1 and the moment t=1. by means of a Fourier series of order 9.

- 1) u(1,1) = 8.71295
- 2) u(1,1) = -0.229174
- 3) u(1,1) = 6.68468
- 4) u(1,1) = -3.52214
- 5) u(1,1) = 4.49927

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 9 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 2, \quad 0 < t \\ u \left(0, t \right) = u \left(2, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{bmatrix} x & 0 \le x \le 1 \\ 2 - x & 1 \le x \le 2 \end{bmatrix} & 0 \le x \le 2 \\ 0 & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point $x = \frac{8}{5}$

and the moment t=0.5 by means of a Fourier series of order 9.

1)
$$u(\frac{8}{5}, 0.5) = 1.93447$$

2)
$$u(\frac{8}{5}, 0.5) = 5.16904$$

3)
$$u(\frac{8}{5}, 0.5) = 7.17637 \times 10^{-6}$$

4)
$$u(\frac{8}{5}, 0.5) = 7.68318$$

5)
$$u(\frac{8}{5}, 0.5) = -3.97872$$

Exercise 2

$$\begin{bmatrix} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{X}, \mathbf{t} \right) = \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{X}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \begin{bmatrix} -\mathbf{x} & 0 \le \mathbf{x} \le \mathbf{2} \\ \mathbf{8} - \mathbf{5} \mathbf{x} & 2 \le \mathbf{x} \le \mathbf{3} & 0 \le \mathbf{x} \le \pi \\ \frac{7 \mathbf{x}}{\pi - \mathbf{3}} - \frac{21}{\pi - \mathbf{3}} - \mathbf{7} & \mathbf{3} \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=1. by means of a Fourier series of order 9.

1)
$$u(2,1) = 0.920717$$

2)
$$u(2,1) = -4.95915$$

3)
$$u(2,1) = -4.33248$$

4)
$$u(2,1) = -2.58769$$

5)
$$u(2,1) = 0.954128$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = \frac{\partial^2 u}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = \begin{cases} 7x & 0 \le x \le 1 \\ 14 - 7x & 1 \le x \le 3 \\ \frac{7x}{\pi - 3} - \frac{21}{\pi - 3} - 7 & 3 \le x \le \pi \end{cases} \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.1 by means of a Fourier series of order 9.

- 1) u(1,0.1) = -5.87844
- 2) u(1,0.1) = -1.65636
- 3) u(1,0.1) = -3.43123
- 4) u(1,0.1) = 4.50226
- 5) u(1,0.1) = -3.71815

Exercise 2

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & \mathbf{0} < \mathbf{x} < \pi, \ \mathbf{0} < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\pi, \mathbf{t} \right) = \mathbf{0} & \mathbf{0} \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \mathbf{2} \left(\mathbf{x} - \mathbf{1} \right) \mathbf{x} \left(\mathbf{x} - \pi \right) & \mathbf{0} \le \mathbf{x} \le \pi \\ \mathbf{0} & \mathbf{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.7 by means of a Fourier series of order 10.

- 1) u(1,0.7) = 0.22016
- 2) u(1,0.7) = 0.516567
- 3) u(1,0.7) = -2.64668
- 4) u(1,0.7) = -3.20267
- 5) u(1,0.7) = -1.17676

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 4 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 3, \ 0 < t \\ u \left(0, t \right) = u \left(3, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{cases} 8 & x & 0 \le x \le 1 \\ 12 - 4 & x & 1 \le x \le 3 \end{cases} & 0 \le x \le 3 \\ 0 & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.6 by means of a Fourier series of order 11.

- 1) u(2,0.6) = -8.21442
- 2) u(2,0.6) = 0.393583
- 3) u(2,0.6) = 6.69195
- 4) u(2,0.6) = -5.32633
- 5) u(2,0.6) = 6.87134

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = 25 \frac{\partial^2 u}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \mathbf{1}, \ 0 < \mathbf{t} \\ \frac{\partial u}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial u}{\partial \mathbf{x}} \left(\mathbf{1}, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = -2 \left(\mathbf{x} - \mathbf{1} \right)^2 \left(\mathbf{x} - \frac{2}{5} \right) \left(\mathbf{x} - \frac{1}{10} \right) \mathbf{x}^2 & 0 \le \mathbf{x} \le \mathbf{1} \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point $x\!=\!\frac{3}{10}$

and the moment t=0.1 by means of a Fourier series of order 10.

1)
$$u(\frac{3}{10}, 0.1) = 3.79966$$

2)
$$u(\frac{3}{10}, 0.1) = 2.1482$$

3)
$$u\left(\frac{3}{10}, 0.1\right) = 2.90479$$

4)
$$u\left(\frac{3}{10}, 0.1\right) = -0.00504762$$

5)
$$u(\frac{3}{10}, 0.1) = 2.3119$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = \mathbf{16} \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{cases} 4 x & 0 \le x \le 1 \\ 11 - 7 x & 1 \le x \le 2 \\ \frac{3 x}{\pi - 2} - \frac{6}{\pi - 2} - 3 & 2 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.8 by means of a Fourier series of order 11.

1)
$$u(1,0.8) = 7.4176 \times 10^{-7}$$

2)
$$u(1,0.8) = -7.00553$$

3)
$$u(1,0.8) = -4.09945$$

4)
$$u(1,0.8) = -5.37623$$

5)
$$u(1,0.8) = -0.938668$$

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 16 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (\pi,t) = 0 & 0 \le t \\ u(x,\theta) = \begin{cases} \frac{5x}{3} & 0 \le x \le 3 \\ -\frac{5x}{\pi-3} + \frac{15}{\pi-3} + 5 & 3 \le x \le \pi \end{cases} & 0 \le x \le \pi \end{cases}$$

$$\theta = 0 \qquad True$$

Compute the temperature of the bar at the point x=1 and the moment t=0.4 by means of a Fourier series of order 11.

1)
$$u(1,0.4) = -1.05421$$

2)
$$u(1,0.4) = 2.49831$$

3)
$$u(1,0.4) = -1.484$$

4)
$$u(1,0.4) = -1.82627$$

5)
$$u(1,0.4) = -4.56858$$

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = \frac{\partial^2 u}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \quad 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \leq \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = -3 \left(\mathbf{x} - \mathbf{2} \right) \ \mathbf{x}^2 \left(\mathbf{x} - \pi \right) & 0 \leq \mathbf{x} \leq \pi \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.7 by means of a Fourier series of order 10.

- 1) u(2,0.7) = -0.928226
- 2) u(2,0.7) = -2.28255
- 3) u(2,0.7) = -8.99664
- 4) u(2,0.7) = 3.37929
- 5) u(2,0.7) = 5.72354

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 16 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 5, \ 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (5,t) = 0 & 0 \le t \\ u(x,\theta) = \begin{cases} \frac{9x}{3} - \frac{5x}{3} & 1 \le x \le 4 & 0 \le x \le 5 \\ 20 - 4x & 4 \le x \le 5 \end{cases} \\ \theta & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=3 and the moment t=0.5 by means of a Fourier series of order 10.

- 1) u(3,0.5) = 4.15268
- 2) u(3,0.5) = -4.96519
- 3) u(3,0.5) = 2.40816
- 4) u(3,0.5) = 5.17683
- 5) u(3,0.5) = -1.32957

Exercise 1

$$\begin{bmatrix} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = 4 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \quad 0 < \mathbf{t} \\ \mathbf{u} \left(\mathbf{0}, \mathbf{t} \right) = \mathbf{u} \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \leq \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \left(\mathbf{x} - \mathbf{2} \right) \left(\mathbf{x} - \mathbf{1} \right) \ \mathbf{x}^2 \left(\mathbf{x} - \pi \right) & 0 \leq \mathbf{x} \leq \pi \\ \mathbf{0} & \text{True} \\ \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.4 by means of a Fourier series of order 11.

- 1) u(2,0.4) = 2.79061
- 2) u(2,0.4) = -7.61248
- 3) u(2,0.4) = -0.0912649
- 4) u(2,0.4) = -3.99676
- 5) u(2,0.4) = 7.20145

Exercise 2

$$\begin{cases} \frac{\partial^2 u}{\partial t^2} \left(x, t \right) = 9 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & \theta < x < \pi, \ \theta < t \\ u \left(\theta, t \right) = u \left(\pi, t \right) = \theta & \theta \le t \\ u \left(x, \theta \right) = \begin{cases} 3 & x & \theta \le x \le 1 \\ 9 - 6 & x & 1 \le x \le 3 \\ \frac{9 x}{\pi - 3} - \frac{27}{\pi - 3} - 9 & 3 \le x \le \pi \end{cases} \\ \frac{\partial}{\partial t} u \left(x, \theta \right) = \begin{cases} -6 & x & \theta \le x \le 1 \\ \frac{6 x}{\pi - 1} - \frac{6}{\pi - 1} - 6 & 1 \le x \le \pi \end{cases} \\ \theta & \text{True}$$

Compute the position of the string at x=1 and the moment t=0.1 by means of a Fourier series of order 8.

- 1) u(1,0.1) = -8.87871
- 2) u(1,0.1) = 0.965097
- 3) u(1,0.1) = 0.0609169
- 4) u(1,0.1) = 6.09684
- 5) u(1,0.1) = -6.83887

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 2, \ 0 < t \\ u \left(0, t \right) = u \left(2, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = 2 \left(x - 2 \right) \left(x - 1 \right) x & 0 \le x \le 2 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point $x\!=\!\frac{6}{5}$

and the moment $t=0.5\,$ by means of a Fourier series of order 12.

1)
$$u(\frac{6}{5}, 0.5) = 2.66632$$

2)
$$u(\frac{6}{5}, 0.5) = 0$$

3)
$$u(\frac{6}{5}, 0.5) = -7.64745$$

4)
$$u(\frac{6}{5}, 0.5) = 2.22037$$

5)
$$u(\frac{6}{5}, 0.5) = -1.31904$$

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 25 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, & 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (\pi,t) = 0 & 0 \le t \\ u(x,\theta) = \begin{cases} -\frac{3x}{2} & 0 \le x \le 2 \\ \frac{3x}{\pi-2} - \frac{6}{\pi-2} - 3 & 2 \le x \le \pi \end{cases}$$

$$0 & True$$

Compute the temperature of the bar at the point x=2 and the moment t=0.5 by means of a Fourier series of order 10.

- 1) u(2,0.5) = -0.50481
- 2) u(2,0.5) = 0.612166
- 3) u(2,0.5) = -1.5
- 4) u(2,0.5) = 4.38158
- 5) u(2,0.5) = -4.02862

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \quad 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = - \left(\left(x - 3 \right) \left(x - 1 \right) \right. \left. x^2 \left(x - \pi \right)^2 \right) & 0 \le x \le \pi \\ 0 & True \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.1 by means of a Fourier series of order 8.

- 1) u(2,0.1) = 0.552374
- 2) u(2,0.1) = -2.14447
- 3) u(2,0.1) = -7.94032
- 4) u(2,0.1) = -0.443218
- 5) u(2,0.1) = -4.01407

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 5, \ 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (5,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} \frac{x}{2} & 0 \le x \le 2 \\ \frac{5}{3} - \frac{x}{3} & 2 \le x \le 5 \end{cases} & 0 < x \le 5 \end{cases}$$

$$\theta = 0 \qquad \qquad \text{True}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.9 by means of a Fourier series of order 10.

- 1) u(2,0.9) = -0.0673694
- 2) u(2,0.9) = -1.20928
- 3) u(2,0.9) = 4.72864
- 4) u(2,0.9) = -4.36103
- 5) u(2,0.9) = 0.597614

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 2, \ 0 < t \\ u \left(0, t \right) = u \left(2, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = 3 \left(x - 2 \right) \left(x - 1 \right) x^2 & 0 \le x \le 2 \\ 0 & True \end{bmatrix}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.9 by means of a Fourier series of order 8.

- 1) u(1,0.9) = 0
- 2) u(1,0.9) = -8.81962
- 3) u(1,0.9) = -6.78561
- 4) u(1,0.9) = 6.49009
- 5) u(1,0.9) = -3.61494

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} \left(\mathbf{x}, \mathbf{t} \right) = 4 \frac{\partial^{2} u}{\partial x^{2}} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = 3 \left(\mathbf{x} - \mathbf{1} \right) \ \mathbf{x}^{2} \left(\mathbf{x} - \pi \right) & 0 \le \mathbf{x} \le \pi \\ \frac{\partial}{\partial \mathbf{t}} u \left(\mathbf{x}, \mathbf{0} \right) = 3 \left(\mathbf{x} - \mathbf{3} \right) \ \mathbf{x}^{2} \left(\mathbf{x} - \pi \right)^{2} & \mathbf{0} . \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the position of the string at x=1 and the moment t=1. by means of a Fourier series of order 9.

- 1) u(1,1) = 2.29969
- 2) u(1,1) = -4.73245
- 3) u(1,1) = -0.964586
- 4) u(1,1.) = -11.3171
- 5) u(1,1) = -7.84525

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x \text{,} t \right) = 16 \frac{\partial^2 u}{\partial x^2} \left(x \text{,} t \right) & \text{0} < x < 2 \text{, 0} < t \\ u \left(\theta \text{,} t \right) = u \left(2 \text{,} t \right) = 0 & \text{0} \le t \\ u \left(x \text{,} \theta \right) = \begin{bmatrix} 2 & x & \text{0} \le x \le 1 \\ 4 - 2 & x & 1 \le x \le 2 \end{bmatrix} & \text{0} \le x \le 2 \\ \theta & \text{True}$$

Compute the temperature of the bar at the point $x\!=\!\begin{array}{c} 6\\ -\\ 5\end{array}$

and the moment t=0.8 by means of a Fourier series of order 8.

1)
$$u(\frac{6}{5}, 0.8) = 0$$

2)
$$u(\frac{6}{5}, 0.8) = 5.50791$$

3)
$$u(\frac{6}{5}, 0.8) = -8.16421$$

4)
$$u(\frac{6}{5}, 0.8) = 7.99527$$

5)
$$u(\frac{6}{5}, 0.8) = 6.7965$$

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} (x,t) = 16 \frac{\partial^{2} u}{\partial x^{2}} (x,t) & 0 < x < \pi, \ \theta < t \\ u(\theta,t) = u(\pi,t) = 0 & 0 \le t \\ u(x,\theta) = \begin{cases} -\frac{5x}{3} & 0 \le x \le 3 \\ \frac{5x}{\pi-3} - \frac{15}{\pi-3} - 5 & 3 \le x \le \pi \end{cases} & 0 \le x \le \pi \\ \frac{\partial}{\partial t} u(x,\theta) = \begin{cases} 7x & 0 \le x \le 1 \\ 14 - 7x & 1 \le x \le 3 \\ \frac{7x}{\pi-3} - \frac{21}{\pi-3} - 7 & 3 \le x \le \pi \end{cases} & 0.5$$

Compute the position of the string at x=2 and the moment t=0.2 by means of a Fourier series of order 11.

1)
$$u(2,0.2) = 1.05968$$

2)
$$u(2,0.2) = -3.61979$$

3)
$$u(2,0.2) = -1.11561$$

4)
$$u(2,0.2) = -1.65935$$

5)
$$u(2,0.2) = -5.71678$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 4 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 4, \ 0 < t \\ u(0,t) = u(4,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -\frac{x}{3} & 0 \le x \le 3 \\ x - 4 & 3 \le x \le 4 \end{cases} & 0 \le x \le 4 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.7 by means of a Fourier series of order 11.

- 1) u(1,0.7) = -4.15856
- 2) u(1,0.7) = -7.55528
- 3) u(1,0.7) = -8.59342
- 4) u(1,0.7) = -0.0958014
- 5) u(1,0.7) = -2.60101

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} \left(x, t \right) = \frac{\partial^{2} u}{\partial x^{2}} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \leq t \\ u \left(x, 0 \right) = -3 \left(x - 3 \right) x^{2} \left(x - \pi \right)^{2} & 0 \leq x \leq \pi \\ \frac{\partial}{\partial t} u \left(x, 0 \right) = \begin{cases} \frac{9 \, x}{2} & 0 \leq x \leq 2 \\ -\frac{9 \, x}{\pi - 2} + \frac{18}{\pi - 2} + 9 & 2 \leq x \leq \pi \end{cases} & 0 \leq x \leq \pi \end{cases}$$

Compute the position of the string at x=1 and the moment t=0.7 by means of a Fourier series of order 8.

- 1) u(1,0.7) = 8.96441
- 2) u(1,0.7) = 7.16669
- 3) u(1,0.7) = 17.7389
- 4) u(1,0.7) = -8.33958
- 5) u(1,0.7) = 4.20125

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 4 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = 3 \left(x - 3 \right) \left(x - 2 \right) x^2 \left(x - \pi \right)^2 & 0 \le x \le \pi \\ 0 & True \\ \end{bmatrix}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.6 by means of a Fourier series of order 10.

- 1) u(1,0.6) = -8.14445
- 2) u(1,0.6) = 5.8184
- 3) u(1,0.6) = 1.09089
- 4) u(1,0.6) = -5.46285
- 5) u(1,0.6) = -3.85323

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ \frac{\partial u}{\partial x} \left(0, t \right) = \frac{\partial u}{\partial x} \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = -2 \left(x - 3 \right) \left(x - 1 \right) x \left(x - \pi \right) & 0 \le x \le \pi \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.9 by means of a Fourier series of order 8.

- 1) u(2,0.9) = 4.30733
- 2) u(2,0.9) = -1.50276
- 3) u(2,0.9) = 3.02814
- 4) u(2,0.9) = -0.160334
- 5) u(2,0.9) = 1.91731

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 5, \ 0 < t \\ u(0,t) = u(5,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -4x & 0 \le x \le 1 \\ x - 5 & 1 \le x \le 5 \end{cases} & 0 \le x \le 5 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=4 and the moment t=0.2 by means of a Fourier series of order 10.

- 1) u(4,0.2) = -0.999999
- 2) u(4,0.2) = 0.56457
- 3) u(4,0.2) = 7.73911
- 4) u(4,0.2) = -4.76894
- 5) u(4,0.2) = 6.23353

Exercise 2

$$\begin{cases} \frac{\partial^2 u}{\partial t^2} \left(x, t \right) = 9 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 3, \ 0 < t \\ u \left(0, t \right) = u \left(3, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = - \left(\left(x - 3 \right) \right) \left(x - 2 \right) \left(x - 1 \right) x \right) & 0 \le x \le 3 \\ \frac{\partial}{\partial t} u \left(x, 0 \right) = \begin{cases} 2 x & 0 \le x \le 2 \\ 12 - 4 x & 2 \le x \le 3 \\ 0 & \text{True} \end{cases}$$

Compute the position of the string at x=1 and the moment t=1. by means of a Fourier series of order 10.

- 1) u(1,1) = -5.95655
- 2) u(1,1) = -0.00851202
- 3) u(1,1) = -4.62636
- 4) u(1,1) = 7.61794
- 5) u(1,1) = -2.92415

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 9 \frac{\partial^2 u}{\partial x^2} (x,t) & \theta < x < \pi, \theta < t \\ u(\theta,t) = u(\pi,t) = \theta & \theta \le t \end{cases}$$

$$\begin{cases} u(x,\theta) = \begin{cases} \frac{4x}{3} & \theta \le x \le 3 \\ -\frac{4x}{\pi-3} + \frac{12}{\pi-3} + 4 & 3 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.3 by means of a Fourier series of order 12.

- 1) u(2,0.3) = -4.00601
- 2) u(2,0.3) = 3.23886
- 3) u(2,0.3) = 8.72401
- 4) u(2,0.3) = 0.162436
- 5) u(2,0.3) = -3.6447

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 16 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 4, \ 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (4,t) = 0 & 0 \le t \\ u(x,\theta) = -2 (x-4) (x-3) (x-1) x^2 & 0 \le x \le 4 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=3 and the moment t=0.6 by means of a Fourier series of order 10.

- 1) u(3,0.6) = -2.12677
- 2) u(3,0.6) = -2.95829
- 3) u(3,0.6) = -0.487423
- 4) u(3,0.6) = 4.00752
- 5) u(3,0.6) = 0.0346472

Exercise 1

$$\begin{bmatrix} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = 4 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ \mathbf{u} \left(\mathbf{0}, \mathbf{t} \right) = \mathbf{u} \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \leq \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = -3 \left(\mathbf{x} - \mathbf{3} \right) \left(\mathbf{x} - \mathbf{2} \right) \mathbf{x}^2 \left(\mathbf{x} - \pi \right)^2 & 0 \leq \mathbf{x} \leq \pi \\ \mathbf{0} & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.4 by means of a Fourier series of order 9.

- 1) u(1,0.4) = 3.29722
- 2) u(1,0.4) = 7.59604
- 3) u(1,0.4) = -2.44748
- 4) u(1,0.4) = 3.24818
- 5) u(1,0.4) = -1.77384

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 16 \frac{\partial^2 u}{\partial x^2} (x,t) & \theta < x < \pi, \theta < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (\pi,t) = \theta & \theta \le x \le 1 \\ u(x,\theta) = \begin{cases} -2x & \theta \le x \le 1 \\ \frac{2x}{\pi-1} - \frac{2}{\pi-1} - 2 & 1 \le x \le \pi \end{cases} & \theta \le x \le \pi \end{cases}$$

$$\begin{cases} u(x,\theta) = \begin{cases} -2x & \theta \le x \le \pi \\ \frac{\pi}{\pi-1} & -\frac{\pi}{\pi} & 0 \le x \le \pi \end{cases}$$

$$\begin{cases} u(x,\theta) = \frac{\pi}{\pi} & 0 \le x \le \pi \end{cases}$$

$$\begin{cases} u(x,\theta) = \frac{\pi}{\pi} & 0 \le x \le \pi \end{cases}$$

$$\begin{cases} u(x,\theta) = \frac{\pi}{\pi} & 0 \le x \le \pi \end{cases}$$

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$$\begin{cases} u(x,\theta) = \frac{\pi}{\pi} & 0 \le x \le \pi \end{cases}$$

$$\begin{cases} u(x,\theta) = \frac{\pi}{\pi} & 0 \le x \le \pi \end{cases}$$

$$\begin{cases} u(x,\theta) = \frac{\pi}{\pi} & 0 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.3 by means of a Fourier series of order 9.

- 1) u(2,0.3) = 4.2254
- 2) u(2,0.3) = -0.133124
- 3) u(2,0.3) = 1.96717
- 4) u(2,0.3) = -0.998868
- 5) u(2,0.3) = -1.73604

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = \mathbf{16} \frac{\partial^2 u}{\partial x^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \quad 0 < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = - \left(\left(\mathbf{x} - \mathbf{1} \right) \ \mathbf{x}^2 \ \left(\mathbf{x} - \pi \right) \right) & 0 \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \\ \end{bmatrix}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.6 by means of a Fourier series of order 12.

- 1) u(1,0.6) = 0.000179032
- 2) u(1,0.6) = 6.50458
- 3) u(1,0.6) = -7.19974
- 4) u(1,0.6) = 5.98292
- 5) u(1,0.6) = 2.93453

Exercise 2

$$\begin{bmatrix} \frac{\partial^2 u}{\partial t^2} \left(\mathbf{X}, \mathbf{t} \right) = 4 \frac{\partial^2 u}{\partial x^2} \left(\mathbf{X}, \mathbf{t} \right) & \theta < \mathbf{X} < \pi, \ \theta < \mathbf{t} \\ \mathbf{u} \left(\theta, \mathbf{t} \right) = \mathbf{u} \left(\pi, \mathbf{t} \right) = 0 & \theta \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{X}, \mathbf{0} \right) = \begin{bmatrix} -\mathbf{X} & \theta \le \mathbf{X} \le \mathbf{2} \\ 6 - 4 \mathbf{X} & 2 \le \mathbf{X} \le \mathbf{3} \\ \frac{6 \mathbf{X}}{\pi - 3} - \frac{18}{\pi - 3} - 6 & 3 \le \mathbf{X} \le \pi \end{bmatrix} \\ \frac{\partial}{\partial t} \mathbf{u} \left(\mathbf{X}, \mathbf{0} \right) = \mathbf{3} \left(\mathbf{X} - \mathbf{1} \right) \mathbf{X}^2 \left(\mathbf{X} - \pi \right) & \theta . \le \mathbf{X} \le \pi \\ \mathbf{0} & \mathbf{True} \end{bmatrix}$$

Compute the position of the string at x=1 and the moment t=0.2 by means of a Fourier series of order 12.

- 1) u(1,0.2) = -1.11215
- 2) u(1,0.2) = -1.94086
- 3) u(1,0.2) = -6.78568
- 4) u(1,0.2) = 3.56956
- 5) u(1,0.2) = -7.08761

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 25 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 3, 0 < t \\ u(0,t) = u(3,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} 9x & 0 \le x \le 1 \\ 24 - 15x & 1 \le x \le 2 \\ 6x - 18 & 2 \le x \le 3 \end{cases} \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.5 by means of a Fourier series of order 12.

- 1) u(1,0.5) = -8.29144
- 2) u(1,0.5) = -6.08624
- 3) u(1,0.5) = 3.42771
- 4) u(1,0.5) = 6.39204
- 5) $u(1,0.5) = 1.52342 \times 10^{-6}$

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} (x,t) = \frac{\partial^{2} u}{\partial x^{2}} (x,t) & 0 < x < 2, \ 0 < t \\ u (0,t) = u (2,t) = 0 & 0 \le t \\ u (x,0) = 2 (x-2)^{2} (x-1) x & 0 \le x \le 2 \\ \frac{\partial}{\partial t} u (x,0) = 3 (x-2)^{2} (x-1) x & 0 \le x \le 2 \\ 0 & True \end{cases}$$

Compute the position of the string at $x = \frac{19}{10}$

and the moment t=0.9 by means of a Fourier series of order 12.

1)
$$u(\frac{19}{10}, 0.9) = 3.4632$$

2)
$$u(\frac{19}{10}, 0.9) = -2.90864$$

3)
$$u(\frac{19}{10}, 0.9) = -0.126296$$

4)
$$u(\frac{19}{10}, 0.9) = -8.68027$$

5)
$$u(\frac{19}{10}, 0.9) = -1.96973$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = 4 \frac{\partial^2 u}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & \mathbf{0} < \mathbf{x} < \pi, \ \mathbf{0} < \mathbf{t} \\ u \left(\mathbf{0}, \mathbf{t} \right) = u \left(\pi, \mathbf{t} \right) = \mathbf{0} & \mathbf{0} \le \mathbf{t} \\ u \left(\mathbf{x}, \mathbf{0} \right) = - \left(\left(\mathbf{x} - \mathbf{3} \right) \left(\mathbf{x} - \mathbf{1} \right) \mathbf{x} \left(\mathbf{x} - \pi \right)^2 \right) & \mathbf{0} \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.8 by means of a Fourier series of order 11.

- 1) u(2,0.8) = 0.0436832
- 2) u(2,0.8) = -7.83177
- 3) u(2,0.8) = 8.01294
- 4) u(2,0.8) = 6.59035
- 5) u(2,0.8) = -4.38274

Exercise 2

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} (\mathbf{x}, \mathbf{t}) = 25 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} (\mathbf{x}, \mathbf{t}) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} (\mathbf{0}, \mathbf{t}) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} (\pi, \mathbf{t}) = \mathbf{0} & 0 \le \mathbf{t} \\ \mathbf{u} (\mathbf{x}, \mathbf{0}) = -\left((\mathbf{x} - \mathbf{3}) \ \mathbf{x}^2 \ (\mathbf{x} - \pi)^2 \right) & 0 \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.4 by means of a Fourier series of order 11.

- 1) u(2,0.4) = 4.64054
- 2) u(2,0.4) = -2.18163
- 3) u(2,0.4) = -3.7034
- 4) u(2,0.4) = -1.85987
- 5) u(2,0.4) = 3.00744

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} \left(x, t \right) = 9 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 2, \quad 0 < t \\ u \left(0, t \right) = u \left(2, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \left(x - 2 \right)^2 \left(x - 1 \right) x & 0 \le x \le 2 \\ 0 & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.2 by means of a Fourier series of order 9.

- 1) u(1,0.2) = -0.00166057
- 2) u(1,0.2) = 3.75838
- 3) u(1,0.2) = 5.12674
- 4) u(1,0.2) = -1.32726
- 5) u(1,0.2) = -3.15936

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} (x,t) = 9 \frac{\partial^{2} u}{\partial x^{2}} (x,t) & 0 < x < 4, \ 0 < t \\ u (0,t) = u (4,t) = 0 & 0 \le t \\ u (x,0) = \begin{cases} -8 x & 0 \le x \le 1 \\ 9 x - 17 & 1 \le x \le 2 \\ 2 - \frac{x}{2} & 2 \le x \le 4 \end{cases} & 0 \le x \le 4 \\ \frac{\partial}{\partial t} u (x,0) = -3 (x - 4)^{2} (x - 3) x^{2} & 0 \le x \le 4 \\ 0 & True \end{cases}$$

Compute the position of the string at x=3 and the moment t=0.2 by means of a Fourier series of order 8.

- 1) u(3,0.2) = 6.7487
- 2) u(3,0.2) = -0.900976
- 3) u(3,0.2) = 1.34345
- 4) u(3,0.2) = 8.57248
- 5) u(3,0.2) = 3.90026

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ u(0,t) = u(\pi,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -3x & 0 \le x \le 3 \\ \frac{9x}{\pi-3} - \frac{27}{\pi-3} - 9 & 3 \le x \le \pi \end{cases} & 0 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.4 by means of a Fourier series of order 8.

- 1) u(1,0.4) = 7.5968
- 2) u(1,0.4) = 2.89227
- 3) u(1,0.4) = 1.27537
- 4) u(1,0.4) = -8.72888
- 5) u(1,0.4) = -2.83883

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} (x,t) = 4 \frac{\partial^{2} u}{\partial x^{2}} (x,t) & 0 < x < 5, \ 0 < t \\ u (0,t) = u (5,t) = 0 & 0 \le t \\ u (x,0) = -3 (x-5) (x-2) x^{2} & 0 \le x \le 5 \\ \frac{\partial}{\partial t} u (x,0) = \begin{cases} -2 x & 0 \le x \le 2 \\ 5 x - 14 & 2 \le x \le 3 \\ \frac{5}{2} - \frac{x}{2} & 3 \le x \le 5 \end{cases} \\ 0 & \text{True} \end{cases}$$

Compute the position of the string at x=3 and the moment t=0.2 by means of a Fourier series of order 8.

- 1) u(3,0.2) = 53.3511
- 2) u(3,0.2) = -6.11685
- 3) u(3,0.2) = 1.4439
- 4) u(3,0.2) = 6.55862
- 5) u(3,0.2) = 7.7535

Exercise 1

$$\begin{bmatrix} \frac{\partial \mathbf{u}}{\partial \mathsf{t}} \left(\mathbf{x}, \mathsf{t} \right) = 4 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathsf{t} \right) & 0 < \mathsf{x} < \pi, \ 0 < \mathsf{t} \\ \mathbf{u} \left(\mathbf{0}, \mathsf{t} \right) = \mathbf{u} \left(\pi, \mathsf{t} \right) = \mathbf{0} & 0 \leq \mathsf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = 2 \left(\mathbf{x} - 3 \right) \mathbf{x} \left(\mathbf{x} - \pi \right)^2 & 0 \leq \mathsf{x} \leq \pi \\ \mathbf{0} & \mathsf{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.8 by means of a Fourier series of order 8.

- 1) u(1,0.8) = 5.30374
- 2) u(1,0.8) = -6.57473
- 3) u(1,0.8) = -0.45107
- 4) u(1,0.8) = 1.25799
- 5) u(1,0.8) = -8.34482

Exercise 2

$$\begin{bmatrix} \frac{\partial^{2} u}{\partial t^{2}} (x,t) = 9 \frac{\partial^{2} u}{\partial x^{2}} (x,t) & 0 < x < \pi, 0 < t \\ u(0,t) = u(\pi,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} \frac{5x}{2} & 0 \le x \le 2 \\ -\frac{5x}{\pi-2} + \frac{10}{\pi-2} + 5 & 2 \le x \le \pi \end{cases} & 0 \le x \le \pi \end{bmatrix}$$

$$\frac{\partial}{\partial t} u(x,0) = -2 (x-3) x^{2} (x-\pi)^{2} & 0 \le x \le \pi$$

$$0 = 0 \qquad True$$

Compute the position of the string at x=2 and the moment t=0.4 by means of a Fourier series of order 10.

- 1) u(2,0.4) = 6.39499
- 2) u(2,0.4) = -2.59854
- 3) u(2,0.4) = 4.85048
- 4) u(2,0.4) = -8.33216
- 5) u(2,0.4) = -0.192748

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = 9\frac{\partial^2 u}{\partial x^2}(x,t) & 0 < x < 5, 0 < t \\ u(0,t) = u(5,t) = 0 & 0 \le t \end{cases}$$

$$\begin{cases} u(x,0) = \begin{cases} \frac{x}{2} & 0 \le x \le 4 \\ 10 - 2x & 4 \le x \le 5 \end{cases} & 0 \le x \le 5 \end{cases}$$

$$0 & True$$

Compute the temperature of the bar at the point x=3 and the moment t=0.7 by means of a Fourier series of order 8.

- 1) u(3,0.7) = 0.117754
- 2) u(3,0.7) = -2.47215
- 3) u(3,0.7) = 0.746336
- 4) u(3,0.7) = 5.17642
- 5) u(3,0.7) = 3.20606

Exercise 2

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{X}, \mathbf{t} \right) = \mathbf{16} \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{X}, \mathbf{t} \right) & \mathbf{0} < \mathbf{x} < \pi, \ \mathbf{0} < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\pi, \mathbf{t} \right) = \mathbf{0} & \mathbf{0} \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = -\mathbf{2} \left(\mathbf{x} - \mathbf{2} \right) \left(\mathbf{x} - \mathbf{1} \right) \mathbf{x} \left(\mathbf{x} - \pi \right) & \mathbf{0} \le \mathbf{x} \le \pi \\ \mathbf{0} & \mathsf{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=1. by means of a Fourier series of order 11.

- 1) u(1,1) = -0.527695
- 2) u(1,1) = -3.0709
- 3) u(1,1) = -1.56255
- 4) u(1,1) = -4.35167
- 5) u(1,1) = 0.817507

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = 4 \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < 2, \ 0 < t \\ u \left(0, t \right) = u \left(2, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = 2 \left(x - 2 \right) \left(x - 1 \right) x & 0 \le x \le 2 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point $x = \frac{3}{5}$

and the moment t=0.4 by means of a Fourier series of order 10.

1)
$$u(\frac{3}{5}, 0.4) = -5.59615$$

2)
$$u(\frac{3}{5}, 0.4) = -6.01781$$

3)
$$u(\frac{3}{5}, 0.4) = 1.02062 \times 10^{-7}$$

4)
$$u(\frac{3}{5}, 0.4) = -3.02868$$

5)
$$u(\frac{3}{5}, 0.4) = 3.80837$$

Exercise 2

$$\begin{bmatrix} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & \mathbf{0} < \mathbf{x} < \pi, \ \mathbf{0} < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\pi, \mathbf{t} \right) = \mathbf{0} & \mathbf{0} \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = - \left(\left(\mathbf{x} - \mathbf{3} \right) \ \mathbf{x}^2 \ \left(\mathbf{x} - \pi \right)^2 \right) & \mathbf{0} \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.5 by means of a Fourier series of order 8.

- 1) u(2,0.5) = 3.82826
- 2) u(2,0.5) = -2.17075
- 3) u(2,0.5) = -3.03686
- 4) u(2,0.5) = 4.49939
- 5) u(2,0.5) = 0.682321

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = 9\frac{\partial^2 u}{\partial x^2}(x,t) & 0 < x < 2, \ 0 < t \\ u(0,t) = u(2,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -9x & 0 \le x \le 1 \\ 9x - 18 & 1 \le x \le 2 \end{cases} & 0 \le x \le 2 \\ 0 & \text{True} \end{cases}$$

Compute the temperature of the bar at the point $x = \frac{13}{10}$

and the moment $t\!=\!0.3\,$ by means of a Fourier series of order 9 .

1)
$$u(\frac{13}{10}, 0.3) = -3.80937$$

2)
$$u(\frac{13}{10}, 0.3) = 6.24734$$

3)
$$u(\frac{13}{10}, 0.3) = -0.00831096$$

4)
$$u(\frac{13}{10}, 0.3) = -6.88377$$

5)
$$u(\frac{13}{10}, 0.3) = 4.11457$$

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 25 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 5, \ 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (5,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -6x & 0 \le x \le 1 \\ \frac{3x}{2} - \frac{15}{2} & 1 \le x \le 5 \end{cases} & 0 \le x \le 5 \\ 0 & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=3 and the moment t=0.2 by means of a Fourier series of order 8.

- 1) u(3,0.2) = 3.38795
- 2) u(3,0.2) = 2.08932
- 3) u(3,0.2) = -2.93221
- 4) u(3,0.2) = -3.89055
- 5) u(3,0.2) = 2.64435

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = 16 \frac{\partial^2 u}{\partial x^2}(x,t) & 0 < x < 4, \ 0 < t \\ u(0,t) = u(4,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} 6x & 0 \le x \le 1 \\ 8 - 2x & 1 \le x \le 4 \end{cases} & 0 \le x \le 4 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=3 and the moment t=0.5 by means of a Fourier series of order 9.

- 1) u(3,0.5) = -4.23817
- 2) u(3,0.5) = -5.75638
- 3) u(3,0.5) = 5.34784
- 4) u(3,0.5) = 0.599321
- 5) u(3,0.5) = 0.0233181

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 25 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ \frac{\partial u}{\partial x} (\theta,t) = \frac{\partial u}{\partial x} (\pi,t) = \theta & 0 \le t \\ u(x,\theta) = \begin{bmatrix} -4x & 0 \le x \le 2 \\ \frac{8x}{\pi-2} - \frac{16}{\pi-2} - 8 & 2 \le x \le \pi \end{bmatrix} & 0 \le x \le \pi \\ 0 & \text{True} \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.6 by means of a Fourier series of order 12.

- 1) u(2,0.6) = 3.09309
- 2) u(2,0.6) = 3.12502
- 3) u(2,0.6) = -4.
- 4) u(2,0.6) = 0.0458089
- 5) u(2,0.6) = -1.52384

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = 25 \frac{\partial^{2} u}{\partial x^{2}}(x,t) & 0 < x < 1, 0 < t \\ u(0,t) = u(1,t) = 0 & 0 \le t \end{cases}$$

$$\begin{cases} x & 0 \le x \le \frac{1}{5} \\ u(x,0) = \begin{cases} 5x & 0 \le x \le \frac{1}{5} \\ \frac{5}{3} - \frac{10x}{3} & \frac{1}{5} \le x \le \frac{4}{5} & 0 \le x \le 1 \\ 5x - 5 & \frac{4}{5} \le x \le 1 \end{cases}$$

Compute the temperature of the bar at the point $x = \frac{1}{5}$ and the moment t = 0.4 by means of a Fourier series of order 11.

1)
$$u(\frac{1}{5}, 0.4) = -2.46133$$

2)
$$u(\frac{1}{5}, 0.4) = 6.33952$$

3)
$$u(\frac{1}{5}, 0.4) = -6.37823$$

4)
$$u(\frac{1}{5}, 0.4) = -5.32019$$

5)
$$u(\frac{1}{5}, 0.4) = 0$$

Exercise 2

$$\begin{bmatrix} \frac{\partial^2 u}{\partial t^2} (x,t) = \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 1, \ 0 < t \\ u(0,t) = u(1,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} 10 & x & 0 \le x \le \frac{1}{2} \\ 20 - 30 & x & \frac{1}{2} \le x \le \frac{4}{5} \\ 20 & x - 20 & \frac{4}{5} \le x \le 1 \end{cases} & 0 \le x \le 1 \\ \frac{\partial}{\partial t} u(x,0) = \begin{cases} -20 & x & 0 \le x \le \frac{3}{10} \\ \frac{60 & x}{7} - \frac{60}{7} & \frac{3}{10} \le x \le 1 \\ 0 & \text{True} \end{cases}$$

Compute the position of the string at $x = \frac{4}{5}$

and the moment t=0.9 by means of a Fourier series of order 9.

1)
$$u(\frac{4}{5}, 0.9) = 6.25619$$

2)
$$u(\frac{4}{5}, 0.9) = -0.546324$$

3)
$$u(\frac{4}{5}, 0.9) = -2.38908$$

4)
$$u(\frac{4}{5}, 0.9) = -1.01762$$

5)
$$u(\frac{4}{5}, 0.9) = 5.58228$$

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 25 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ u(0,t) = u(\pi,t) = 0 & 0 \le t \end{cases}$$

$$u(x,0) = \begin{cases} -\frac{9x}{2} & 0 \le x \le 2 \\ x - 11 & 2 \le x \le 3 & 0 \le x \le \pi \\ \frac{8x}{\pi - 3} - \frac{24}{\pi - 3} - 8 & 3 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=1. by means of a Fourier series of order 9.

- 1) u(2,1.) = -4.38304
- 2) u(2,1) = -3.96968
- 3) u(2,1.) = 6.38601
- 4) $u(2,1.) = -1.03172 \times 10^{-10}$
- 5) u(2,1.) = 7.19324

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} \left(\mathbf{X}, \mathbf{t} \right) = \frac{\partial^{2} u}{\partial x^{2}} \left(\mathbf{X}, \mathbf{t} \right) & 0 < \mathbf{X} < \pi, \ 0 < \mathbf{t} \\ \mathbf{u} \left(\mathbf{0}, \mathbf{t} \right) = \mathbf{u} \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \leq \mathbf{t} \\ \mathbf{u} \left(\mathbf{X}, \mathbf{0} \right) = \begin{cases} -2 \mathbf{X} & 0 \leq \mathbf{X} \leq 3 \\ \frac{6 \mathbf{X}}{\pi - 3} - \frac{18}{\pi - 3} - 6 & 3 \leq \mathbf{X} \leq \pi \end{cases} & 0 \leq \mathbf{X} \leq \pi \\ \frac{\partial}{\partial t} \mathbf{u} \left(\mathbf{X}, \mathbf{0} \right) = 3 \left(\mathbf{X} - 3 \right) \left(\mathbf{X} - 2 \right) \mathbf{X}^{2} \left(\mathbf{X} - \pi \right)^{2} & \mathbf{0}. \leq \mathbf{X} \leq \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the position of the string at x=1 and the moment t=0.6 by means of a Fourier series of order 11.

- 1) u(1,0.6) = 1.56629
- 2) u(1,0.6) = -2.27133
- 3) u(1,0.6) = -5.28918
- 4) u(1,0.6) = 8.19516
- 5) u(1,0.6) = 11.4186

Exercise 1

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 4 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, & 0 < t \\ u(0,t) = u(\pi,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -8x & 0 \le x \le 1 \\ -\frac{x}{2} - \frac{15}{2} & 1 \le x \le 3 \\ \frac{9x}{\pi - 3} - \frac{27}{\pi - 3} - 9 & 3 \le x \le \pi \end{cases}$$

$$0 & True$$

Compute the temperature of the bar at the point x=2 and the moment t=0.7 by means of a Fourier series of order 12.

1)
$$u(2,0.7) = 3.67274$$

2)
$$u(2,0.7) = 5.8238$$

3)
$$u(2,0.7) = -0.540416$$

4)
$$u(2,0.7) = -2.82516$$

5)
$$u(2,0.7) = -2.75552$$

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}} (x,t) = 4 \frac{\partial^{2} u}{\partial x^{2}} (x,t) & 0 < x < 2, \ 0 < t \\ u (0,t) = u (2,t) = 0 & 0 \le t \\ u (x,0) = -2 (x-2) (x-1) x^{2} & 0 \le x \le 2 \\ \frac{\partial}{\partial t} u (x,0) = \begin{cases} -2x & 0 \le x \le 1 \\ 2x-4 & 1 \le x \le 2 \end{cases} & 0 \cdot \le x \le 2 \\ 0 & \text{True} \end{cases}$$

Compute the position of the string at $x = \frac{9}{5}$

and the moment t=0.9 by means of a Fourier series of order 9.

1)
$$u(\frac{9}{5}, 0.9) = 0.115516$$

2)
$$u(\frac{9}{5}, 0.9) = -8.22627$$

3)
$$u(\frac{9}{5}, 0.9) = 1.1838$$

4)
$$u(\frac{9}{5}, 0.9) = 4.86657$$

5)
$$u(\frac{9}{5}, 0.9) = 1.22366$$

Exercise 1

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} (\mathbf{x}, \mathbf{t}) = 9 \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} (\mathbf{x}, \mathbf{t}) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ \mathbf{u} (\mathbf{0}, \mathbf{t}) = \mathbf{u} (\pi, \mathbf{t}) = \mathbf{0} & 0 \le \mathbf{t} \\ \mathbf{u} (\mathbf{x}, \mathbf{0}) = \begin{cases} -\frac{2x}{3} & 0 \le x \le 3 \\ \frac{2x}{\pi - 3} - \frac{6}{\pi - 3} - 2 & 3 \le x \le \pi \end{cases} & 0 \le \mathbf{x} \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.2 by means of a Fourier series of order 8.

- 1) u(1,0.2) = -3.34055
- 2) u(1,0.2) = 8.77187
- 3) u(1,0.2) = 3.29441
- 4) u(1,0.2) = -2.01062
- 5) u(1,0.2) = -0.184393

Exercise 2

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 9 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (\pi,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -5x & 0 \le x \le 1 \\ -5 & 1 \le x \le 2 \\ \frac{5x}{\pi-2} - \frac{10}{\pi-2} - 5 & 2 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.5 by means of a Fourier series of order 11.

- 1) u(2,0.5) = 3.66857
- 2) u(2,0.5) = -0.897518
- 3) u(2,0.5) = -3.29501
- 4) u(2,0.5) = 0.53619
- 5) u(2,0.5) = 0.747588

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 4 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 3, \ 0 < t \\ u (0,t) = u (3,t) = 0 & 0 \le t \\ u (x,0) = \begin{cases} -2x & 0 \le x \le 1 \\ 9x - 11 & 1 \le x \le 2 & 0 \le x \le 3 \\ 21 - 7x & 2 \le x \le 3 \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.6 by means of a Fourier series of order 11.

- 1) u(1,0.6) = -4.10497
- 2) u(1,0.6) = 0.163926
- 3) u(1,0.6) = -3.32396
- 4) u(1,0.6) = 5.24404
- 5) u(1,0.6) = 8.55142

Exercise 2

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} \left(\mathbf{x}, \mathbf{t} \right) = \mathbf{16} \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & \mathbf{0} < \mathbf{x} < \pi, \ \mathbf{0} < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\pi, \mathbf{t} \right) = \mathbf{0} & \mathbf{0} \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \mathbf{3} \left(\mathbf{x} - \mathbf{3} \right) \left(\mathbf{x} - \mathbf{1} \right) \mathbf{x} \left(\mathbf{x} - \pi \right) & \mathbf{0} \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.2 by means of a Fourier series of order 11.

- 1) u(2,0.2) = 4.50176
- 2) u(2,0.2) = 1.64976
- 3) u(2,0.2) = 4.87685
- 4) u(2,0.2) = -0.805338
- 5) u(2,0.2) = 0.745453

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} \left(x, t \right) = \frac{\partial^2 u}{\partial x^2} \left(x, t \right) & 0 < x < \pi, \ 0 < t \\ u \left(0, t \right) = u \left(\pi, t \right) = 0 & 0 \le t \\ u \left(x, 0 \right) = \begin{cases} 2x & 0 \le x \le 1 \\ -\frac{2x}{\pi - 1} + \frac{2}{\pi - 1} + 2 & 1 \le x \le \pi \end{cases} & 0 \le x \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.2 by means of a Fourier series of order 10.

- 1) u(1,0.2) = 1.26014
- 2) u(1,0.2) = -2.27019
- 3) u(1,0.2) = -0.421383
- 4) u(1,0.2) = -7.69391
- 5) u(1,0.2) = -4.75966

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 3, 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (3,t) = 0 & 0 \le t \\ u(x,0) = \begin{bmatrix} -6x & 0 \le x \le 1 \\ 3x - 9 & 1 \le x \le 3 \end{bmatrix} & 0 \le x \le 3 \\ 0 & True \end{bmatrix}$$

Compute the temperature of the bar at the point x=2 and the moment t=0.9 by means of a Fourier series of order 10.

- 1) u(2,0.9) = 4.69152
- 2) u(2,0.9) = -2.84975
- 3) u(2,0.9) = -3.67428
- 4) u(2,0.9) = 3.34714
- 5) u(2,0.9) = -1.58385

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 4 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 4, \ 0 < t \\ u (0,t) = u (4,t) = 0 & 0 \le t \\ u (x,0) = \begin{cases} -2x & 0 \le x \le 2 \\ 4 - 4x & 2 \le x \le 3 & 0 \le x \le 4 \\ 8x - 32 & 3 \le x \le 4 \end{cases}$$

$$0 \qquad \qquad \text{True}$$

Compute the temperature of the bar at the point x=2 and the moment t=1. by means of a Fourier series of order 12.

- 1) u(2,1) = -6.49053
- 2) u(2,1) = -1.54308
- 3) u(2,1.) = 8.04957
- 4) u(2,1) = 2.58212
- 5) u(2,1.) = -0.4458

Exercise 2

$$\begin{cases} \frac{\partial^{2} u}{\partial t^{2}}(x,t) = \frac{\partial^{2} u}{\partial x^{2}}(x,t) & 0 < x < 4, \ 0 < t \\ u(0,t) = u(4,t) = 0 & 0 \le t \\ u(x,0) = 3(x-4)^{2}(x-1)x^{2} & 0 \le x \le 4 \\ \frac{\partial}{\partial t}u(x,0) = \begin{cases} \frac{5x}{2} & 0 \le x \le 2 \\ 10 - \frac{5x}{2} & 2 \le x \le 4 \end{cases} & 0. \le x \le 4 \\ 0 & True \end{cases}$$

Compute the position of the string at x=2 and the moment t=0.3 by means of a Fourier series of order 10.

- 1) u(2,0.3) = -0.336936
- 2) u(2,0.3) = -3.89599
- 3) u(2,0.3) = -7.83821
- 4) u(2,0.3) = 47.3237
- 5) u(2,0.3) = 6.61745

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (x,t) = 25 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < 1, 0 < t \\ u(0,t) = u(1,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} \frac{20 x}{9} & 0 \le x \le \frac{9}{10} \\ 20 - 20 x & \frac{9}{10} \le x \le 1 \end{cases} & 0 \le x \le 1 \end{cases}$$

Compute the temperature of the bar at the point $x = \frac{7}{10}$

and the moment t=0.7 by means of a Fourier series of order 12.

1)
$$u(\frac{7}{10}, 0.7) = 7.91813$$

2)
$$u(\frac{7}{10}, 0.7) = -2.19266$$

3)
$$u(\frac{7}{10}, 0.7) = -8.77147$$

4)
$$u(\frac{7}{10}, 0.7) = 0$$

5)
$$u(\frac{7}{10}, 0.7) = 5.45783$$

Exercise 2

$$\begin{bmatrix} \frac{\partial^{2} u}{\partial t^{2}} (x,t) = \frac{\partial^{2} u}{\partial x^{2}} (x,t) & 0 < x < 4, 0 < t \\ u (0,t) = u (4,t) = 0 & 0 \le t \\ u (x,0) = -3 (x-4) (x-1) x & 0 \le x \le 4 \\ \frac{\partial}{\partial t} u (x,0) = \begin{cases} 3x & 0 \le x \le 2 \\ 30 - 12x & 2 \le x \le 3 \\ 6x - 24 & 3 \le x \le 4 \end{cases} & 0. \le x \le 4 \\ 0 & True \end{bmatrix}$$

Compute the position of the string at x=3

and the moment t=0.1 by means of a Fourier series of order 11.

- 1) u(3,0.1) = 5.63518
- 2) u(3,0.1) = 5.00406
- 3) u(3,0.1) = -1.10381
- 4) u(3,0.1) = 17.3628
- 5) u(3,0.1) = -7.08254

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t}(x,t) = 9 \frac{\partial^2 u}{\partial x^2}(x,t) & 0 < x < 4, \ 0 < t \\ u(0,t) = u(4,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} \frac{x}{3} & 0 \le x \le 3 \\ 4 - x & 3 \le x \le 4 \end{cases} & 0 \le x \le 4 \\ 0 & True \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=1. by means of a Fourier series of order 9.

- 1) u(1,1) = -1.84286
- 2) u(1,1) = -4.46182
- 3) u(1,1) = 0.691232
- 4) u(1,1) = -3.37908
- 5) u(1,1) = 0.00209723

Exercise 2

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial t} \left(\mathbf{x}, \mathbf{t} \right) = \frac{\partial^2 \mathbf{u}}{\partial \mathbf{x}^2} \left(\mathbf{x}, \mathbf{t} \right) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\mathbf{0}, \mathbf{t} \right) = \frac{\partial \mathbf{u}}{\partial \mathbf{x}} \left(\pi, \mathbf{t} \right) = \mathbf{0} & 0 \le \mathbf{t} \\ \mathbf{u} \left(\mathbf{x}, \mathbf{0} \right) = \left(\mathbf{x} - \mathbf{3} \right) \ \mathbf{x}^2 \ \left(\mathbf{x} - \pi \right) & 0 \le \mathbf{x} \le \pi \\ \mathbf{0} & \text{True} \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.7 by means of a Fourier series of order 10.

- 1) u(1,0.7) = 2.40747
- 2) u(1,0.7) = 3.00308
- 3) u(1,0.7) = -4.35882
- 4) u(1,0.7) = -2.71585
- 5) u(1,0.7) = 0.577084

Exercise 1

$$\begin{cases} \frac{\partial u}{\partial t} (\mathbf{x}, \mathbf{t}) = 9 \frac{\partial^2 u}{\partial x^2} (\mathbf{x}, \mathbf{t}) & 0 < \mathbf{x} < \pi, \ 0 < \mathbf{t} \\ \mathbf{u} (\mathbf{0}, \mathbf{t}) = \mathbf{u} (\pi, \mathbf{t}) = 0 & 0 \le \mathbf{t} \\ \mathbf{u} (\mathbf{x}, \mathbf{0}) = \begin{cases} -\frac{8x}{3} & 0 \le x \le 3 \\ \frac{8x}{\pi - 3} - \frac{24}{\pi - 3} - 8 & 3 \le x \le \pi \end{cases} & 0 \le \mathbf{x} \le \pi \end{cases}$$

Compute the temperature of the bar at the point x=1 and the moment t=0.1 by means of a Fourier series of order 10.

- 1) u(1,0.1) = 6.92858
- 2) u(1,0.1) = -1.75323
- 3) u(1,0.1) = -0.787937
- 4) u(1,0.1) = 5.8844
- 5) u(1,0.1) = 2.26222

Exercise 2

$$\begin{bmatrix} \frac{\partial u}{\partial t} (x,t) = 9 \frac{\partial^2 u}{\partial x^2} (x,t) & 0 < x < \pi, \ 0 < t \\ \frac{\partial u}{\partial x} (0,t) = \frac{\partial u}{\partial x} (\pi,t) = 0 & 0 \le t \\ u(x,0) = \begin{cases} -9 & 0 \le x \le 1 \\ 6 & x - 15 & 1 \le x \le 2 \\ \frac{3 & x}{\pi - 2} - \frac{6}{\pi - 2} - 3 & 2 \le x \le \pi \end{cases}$$

$$0 & True$$

Compute the temperature of the bar at the point x=1 and the moment t=0.1 by means of a Fourier series of order 12.

- 1) u(1,0.1) = -4.35472
- 2) u(1,0.1) = -0.204014
- 3) u(1,0.1) = 2.24319
- 4) u(1,0.1) = 3.20363
- 5) u(1,0.1) = -1.00595