

```
In[18]:= generadortotal[codigo, Table[i, {i, 1, 20}],  
All → True, TextoInicial → "Further Mathematics - 2018/2019",  
Relacion → "Chapter 3 - Test for ", NumSerie → True]
```

Exercise 1

Compute the curvature for $C(t) = \{-2\cos[t], 3\sin[t], 0\}$ at the point $t=3$.

- 1) $k(3) = 2.20626$
- 2) $k(3) = -7.27978$
- 3) $k(3) = -8.55117$
- 4) $k(3) = 8.98423$
- 5) $k(3) = 0.225962$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$$\{-\cos[u] (2 + \cos[v]) + 2\sin[v], (2 + \cos[v]) \sin[u] + 2\sin[v], -\sin[v]\}$$

at the point $(u,v) = (5,1)$.

- 1) $u(5,1) = -4.98043$
- 2) $u(5,1) = -6.31941$
- 3) $u(5,1) = 7.48893$
- 4) $u(5,1) = 2.0518$
- 5) $u(5,1) = 0.00829818$

Exercise 1

Compute the curvature for $C(t) = \{\cos[t] - \sin[t], \cos[t], 3t\}$ at the point $t=1$.

- 1) $k(1) = 1.37488$
- 2) $k(1) = -8.68577$
- 3) $k(1) = 0.0532364$
- 4) $k(1) = -6.12117$
- 5) $k(1) = -3.3282$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$\{(1+v^2)\cos[u] - (1+v^2)\sin[u], (1+v^2)\cos[u], v\}$ at the point $(u,v) = (6,6)$.

- 1) $u(6,6) = -5.63174$
- 2) $u(6,6) = -3.02635$
- 3) $u(6,6) = -2.58728 \times 10^{-6}$
- 4) $u(6,6) = 8.58539$
- 5) $u(6,6) = -2.73253$

Exercise 1

Compute the torsion for $C(t) =$

$$\{t - 2(7 - 2t + 2t^2), 7 - 2t + 2t^2, 3 - 7t + 9t^2 - 2(7 - 2t + 2t^2)\} \text{ at the point } t=7.$$

1) $\tau(7) = 2.0512$

2) $\tau(7) = -1.69123$

3) $\tau(7) = 0$

4) $\tau(7) = -8.80524$

5) $\tau(7) = 8.32278$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$$\{v \cos[u] - 2v \sin[u], v \sin[u], v + 2v \cos[u] - 2v \sin[u]\} \text{ at the point } (u,v) = (0,3).$$

1) $u(0,3) = 6.3149$

2) $u(0,3) = 4.3494$

3) $u(0,3) = 0$

4) $u(0,3) = 4.93788$

5) $u(0,3) = -8.58406$

Exercise 1

Compute the curvature for $C(t) = \{6 \cos[t], -2 \cos[t] + 3 \sin[t], -2 \cos[t]\}$ at the point $t=5$.

- 1) $k(5) = -7.85339$
- 2) $k(5) = 6.37639$
- 3) $k(5) = -1.15222$
- 4) $k(5) = 0.081256$
- 5) $k(5) = 3.58544$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$$\{3 \cos[u] (2 + \cos[v]) - 2 \sin[v], -\cos[u] (2 + \cos[v]) + (2 + \cos[v]) \sin[u] - \sin[v], -\cos[u] (2 + \cos[v]) + \sin[v]\}$$

at the point $(u,v) = (5,2)$.

- 1) $u(5,2) = -1.4061$
- 2) $u(5,2) = 5.84117$
- 3) $u(5,2) = 1.18171$
- 4) $u(5,2) = -0.000504586$
- 5) $u(5,2) = -7.49036$

Exercise 1

Compute the curvature for $C(t) = \{3t + \cos[t] + \sin[t], 2t + \sin[t], t\}$ at the point $t=0$.

- 1) $k(0) = 5.12192$
- 2) $k(0) = 5.39899$
- 3) $k(0) = 0.0238528$
- 4) $k(0) = -6.74747$
- 5) $k(0) = -0.820059$

Exercise 2

Compute the Gauss curvature for $X(u,v) = \{3v + v \cos[u] + v \sin[u], 2v + v \sin[u], v\}$ at the point $(u,v) = (0,-7)$.

- 1) $u(0,-7) = -6.74747$
- 2) $u(0,-7) = -8.68068$
- 3) $u(0,-7) = 0$
- 4) $u(0,-7) = -6.07791$
- 5) $u(0,-7) = 5.12192$

Exercise 1

Compute the torsion for $C(t) =$

$\{\cos[t] + 10\sin[t], 5\sin[t], -\cos[t] - 15\sin[t]\}$ at the point $t=0$.

1) $\tau(0) = 0$

2) $\tau(0) = 8.00283$

3) $\tau(0) = -4.56076$

4) $\tau(0) = -6.41985$

5) $\tau(0) = 5.04423$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$\{\cos[u] (3 + \cos[v]) + 2 (3 + \cos[v]) \sin[u] - 2 \sin[v], (3 + \cos[v]) \sin[u],$
 $-\cos[u] (3 + \cos[v]) - 3 (3 + \cos[v]) \sin[u] + 3 \sin[v]\}$ at the point $(u,v) = (1,0)$.

1) $u(1,0) = 0.0123286$

2) $u(1,0) = -5.00628$

3) $u(1,0) = 4.69179$

4) $u(1,0) = 4.94026$

5) $u(1,0) = 5.04423$

Exercise 1

Compute the curvature for $C(t) = \{2 \cos[t], -8 \cos[t] + \sin[t], 0\}$ at the point $t=3$.

- 1) $k(3) = -0.0461238$
- 2) $k(3) = -0.699634$
- 3) $k(3) = 5.00399$
- 4) $k(3) = 64.2341$
- 5) $k(3) = -0.168956$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$$\{\cos[u] (4 + \cos[v]) - 3 \sin[v], -4 \cos[u] (4 + \cos[v]) + (4 + \cos[v]) \sin[u] + 6 \sin[v], \sin[v]\}$$

at the point $(u,v) = (0,1)$.

- 1) $u(0,1) = 1.14632$
- 2) $u(0,1) = -6.44353$
- 3) $u(0,1) = 5.21371$
- 4) $u(0,1) = 0.00294638$
- 5) $u(0,1) = -0.672538$

Exercise 1

Compute the torsion for $C(t) =$

$\{\cos[t] + 2\sin[t], \sin[t], 2t + \cos[t] + 3\sin[t]\}$ at the point $t=6$.

1) $\tau(6) = 8.39192$

2) $\tau(6) = -3.83007$

3) $\tau(6) = -7.46373$

4) $\tau(6) = -4.22941$

5) $\tau(6) = 0.299419$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$\{\cos[u] + 2\sin[u], \sin[u], v + \cos[u] + 3\sin[u]\}$ at the point $(u,v) = (5,2)$.

1) $u(5,2) = -4.22941$

2) $u(5,2) = 3.74892$

3) $u(5,2) = -0.623256$

4) $u(5,2) = -7.85597$

5) $u(5,2) = 0$

Exercise 1

Compute the torsion for $C(t) = \{t, 6 - 5t + 8t^2, -8 + 13t - 17t^2\}$ at the point $t=6$.

1) $\tau(6) = -6.01407$

2) $\tau(6) = -8.104$

3) $\tau(6) = 0$

4) $\tau(6) = -3.72331$

5) $\tau(6) = -1.8132$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$\{\cos[u], -v + \cos[u], v + \sin[u]\}$ at the point $(u,v) = (0,4)$.

1) $u(0,4) = -0.95048$

2) $u(0,4) = -4.12787$

3) $u(0,4) = 0$

4) $u(0,4) = -2.88512$

5) $u(0,4) = 7.64698$

Exercise 1

Compute the curvature for $C(t) = \{2t + \cos[t] + \sin[t], -\cos[t], 2t\}$ at the point $t=2$.

- 1) $k(2) = -1.13689$
- 2) $k(2) = 0.107209$
- 3) $k(2) = 1.27778$
- 4) $k(2) = -2.38817$
- 5) $k(2) = 7.92436$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$\{v + v \cos[u] + v \sin[u], -v \cos[u], v\}$ at the point $(u,v) = (5,-2)$.

- 1) $u(5,-2) = 7.92436$
- 2) $u(5,-2) = 0$
- 3) $u(5,-2) = 4.70653$
- 4) $u(5,-2) = -8.55703$
- 5) $u(5,-2) = -1.13689$

Exercise 1

Compute the torsion for $C(t) = \{5 \cos[t] + 2 \sin[t], \sin[t], 0\}$ at the point $t=3$.

- 1) $\tau(3) = 1.67377$
- 2) $\tau(3) = 3.51282$
- 3) $\tau(3) = 1.81089$
- 4) $\tau(3) = 6.3376$
- 5) $\tau(3) = 0$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$$\{-14 + 8u^2 + 8v - 6v^2 + u(-1 + 14v), -7 + 4u^2 + 4v - 3v^2 + u(-1 + 7v), 7 + u - 4u^2 - 3v - 7uv + 3v^2\}$$

at the point $(u,v) = (-5,-8)$.

- 1) $u(-5,-8) = -2.89498$
- 2) $u(-5,-8) = 5.79941$
- 3) $u(-5,-8) = -5.38819$
- 4) $u(-5,-8) = -6.68981$
- 5) $u(-5,-8) = -3.3515 \times 10^{-8}$

Exercise 1

Compute the curvature for $C(t) =$

$$\{t - 2(-9 - 5t - 5t^2), -3 + 2t + 6t^2 + 3(-9 - 5t - 5t^2), 3 - 3t - 6t^2\} \text{ at the point } t=3.$$

1) $k(3) = 0.000119993$

2) $k(3) = -1.44944$

3) $k(3) = 1.76381$

4) $k(3) = -8.20749$

5) $k(3) = 4.72633$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$$\{u - 2v, 8 - 5u^2 + 6v + uv + 2v^2, -8 + 5u^2 - 3v - 2v^2 - u(1+v)\} \text{ at the point } (u,v) = (-5,4).$$

1) $u(-5,4) = -1.03163 \times 10^{-8}$

2) $u(-5,4) = -4.23554$

3) $u(-5,4) = 4.72633$

4) $u(-5,4) = 1.90524$

5) $u(-5,4) = -8.18402$

Exercise 1

Compute the curvature for $C(t) = \{-2 - 4t - 3t^2, 2 + 3t + 3t^2, -6 + 3t - 5t^2\}$ at the point $t=10$.

1) $k(10) = -1.57071$

2) $k(10) = 0.0000326965$

3) $k(10) = -6.33917$

4) $k(10) = -8.47965$

5) $k(10) = -6.50977$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$\{u + v, -2u - v, 5 + 5u^2 + 3v - 3u(1 + v)\}$ at the point $(u,v) = (2,-2)$.

1) $u(2,-2) = 3.22503$

2) $u(2,-2) = -3.9057 \times 10^{-6}$

3) $u(2,-2) = 4.90438$

4) $u(2,-2) = -3.92501$

5) $u(2,-2) = -7.49508$

Exercise 1

Compute the curvature for $C(t) = \{9t + 4(-3 - t - 3t^2), -3 + t - 3t^2, -2 + 4t + 6t^2\}$ at the point $t=1$.

- 1) $k(1) = -3.60401$
- 2) $k(1) = 1.99965$
- 3) $k(1) = 0.00984903$
- 4) $k(1) = 7.77763$
- 5) $k(1) = 3.09602$

Exercise 2

Compute the Gauss curvature for $X(u,v) = \{9(1+3v^2)\cos[u] + 4(1+3v^2)\sin[u], 2(1+3v^2)\cos[u] + (1+3v^2)\sin[u], v - (1+3v^2)\cos[u]\}$ at the point $(u,v) = (3,-6)$.

- 1) $u(3,-6) = -8.00381$
- 2) $u(3,-6) = 5.98001$
- 3) $u(3,-6) = -1.16263 \times 10^{-10}$
- 4) $u(3,-6) = 5.83177$
- 5) $u(3,-6) = 1.99965$

Exercise 1

Compute the curvature for $C(t) = \{\cos[t], \sin[t], t - \sin[t]\}$ at the point $t=3$.

- 1) $k(3) = -2.75567$
- 2) $k(3) = -1.82926$
- 3) $k(3) = 8.28143$
- 4) $k(3) = -0.735959$
- 5) $k(3) = 0.202014$

Exercise 2

Compute the Gauss curvature for $X(u,v) = \{v \cos[u], v \sin[u], v - v \sin[u]\}$ at the point $(u,v) = (1,-9)$.

- 1) $u(1,-9) = -6.6976$
- 2) $u(1,-9) = -0.735959$
- 3) $u(1,-9) = -2.75567$
- 4) $u(1,-9) = -3.86017$
- 5) $u(1,-9) = 0$

Exercise 1

Compute the torsion for $C(t) = \{t, 4 - 5t - 8t^2, -4 - 5t - 7t^2\}$ at the point $t=10$.

- 1) $\tau(10) = -7.30991$
- 2) $\tau(10) = -2.45986$
- 3) $\tau(10) = 6.60069$
- 4) $\tau(10) = 0$
- 5) $\tau(10) = 3.19211$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$$\left\{ \begin{aligned} &\cos[u] (3 + \cos[v]), \cos[u] (3 + \cos[v]) + (3 + \cos[v]) \sin[u] + \sin[v], \\ &-\cos[u] (3 + \cos[v]) + \sin[v] \end{aligned} \right\} \text{ at the point } (u,v) = (1,1).$$

- 1) $u(1,1) = -2.17149$
- 2) $u(1,1) = -6.89571$
- 3) $u(1,1) = 2.33877$
- 4) $u(1,1) = 0.923319$
- 5) $u(1,1) = -4.5031$

Exercise 1

Compute the curvature for $C(t) =$

$\{2 + 7t + 3t^2 - 2(9 + 5t - 6t^2), 9 + 5t - 6t^2, -2 - 6t - 3t^2\}$ at the point $t=8$.

- 1) $k(8) = -4.74944$
- 2) $k(8) = 0.00001431$
- 3) $k(8) = -8.51915$
- 4) $k(8) = -8.31842$
- 5) $k(8) = -6.9327$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$\{-v + \cos[u] - 2\sin[u], \sin[u], v\}$ at the point $(u,v) = (1,2)$.

- 1) $u(1,2) = -6.9327$
- 2) $u(1,2) = 0$
- 3) $u(1,2) = 3.32095$
- 4) $u(1,2) = 7.83623$
- 5) $u(1,2) = 2.90336$

Exercise 1

Compute the torsion for $C(t) = \{t, 7 + 2t^2, -2 - t - 4t^2\}$ at the point $t=4$.

- 1) $\tau(4) = -3.83808$
- 2) $\tau(4) = 0$
- 3) $\tau(4) = -8.57817$
- 4) $\tau(4) = -0.553704$
- 5) $\tau(4) = -3.26266$

Exercise 2

Compute the Gauss curvature for $X(u,v) = \{(1 + 3v^2) \cos[u], -v + (1 + 3v^2) \sin[u], v\}$ at the point $(u,v) = (3, -5)$.

- 1) $u(3, -5) = -2.90225$
- 2) $u(3, -5) = -9.54431 \times 10^{-8}$
- 3) $u(3, -5) = -6.56265$
- 4) $u(3, -5) = 8.03969$
- 5) $u(3, -5) = -3.83808$

Exercise 1

Compute the curvature for $C(t) =$

$\{-4t - 3\cos[t] - \sin[t], -\cos[t] + 2\sin[t], 2t + 2\cos[t]\}$ at the point $t=0$.

1) $k(0) = 0.0693829$

2) $k(0) = -3.43983$

3) $k(0) = -4.0908$

4) $k(0) = 1.63694$

5) $k(0) = 1.85945$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$\{-2v - 3v\cos[u] - v\sin[u], -v\cos[u] + 2v\sin[u], v + 2v\cos[u]\}$ at the point $(u,v) = (4,3)$.

1) $u(4,3) = 0$

2) $u(4,3) = 3.60359$

3) $u(4,3) = 1.83783$

4) $u(4,3) = 8.48301$

5) $u(4,3) = -8.69754$

Exercise 1

Compute the curvature for $C(t) =$

$\{-t + \cos[t], -2t + 4\cos[t] + \sin[t], -t + 2\cos[t]\}$ at the point $t=3$.

- 1) $k(3) = 2.68232$
- 2) $k(3) = -3.55821$
- 3) $k(3) = -8.00121$
- 4) $k(3) = 0.0407095$
- 5) $k(3) = -7.55642$

Exercise 2

Compute the Gauss curvature for $X(u,v) =$

$\{-v + v\cos[u], -2v + 4v\cos[u] + v\sin[u], -v + 2v\cos[u]\}$ at the point $(u,v) = (3,6)$.

- 1) $u(3,6) = 0.812819$
- 2) $u(3,6) = 2.26384$
- 3) $u(3,6) = 6.25744$
- 4) $u(3,6) = 0$
- 5) $u(3,6) = -8.00121$